

Controller Compilation and Compression for Resource Constrained Applications

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International Conference on Algorithmic Decision Theory
Bruxelles, November 13–15, 2013

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POMDP—Example



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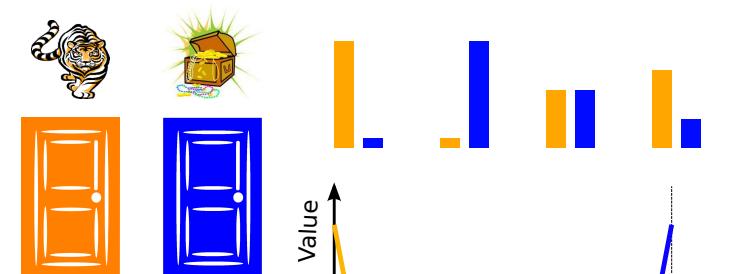
POMDP

Partially Observable Markov Decision Process

- ▶ a discrete time, dynamical system with controls (actions)
- ▶ a policy of action optimises a utility function
- ▶ the state of the system is partially observable through noisy sensors

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POMDP—Example



- ▶ 2 states (tiger left or right)
- ▶ 2 noisy observations (tiger left or tiger right)
- ▶ 3 actions (listen, open left, and open right)

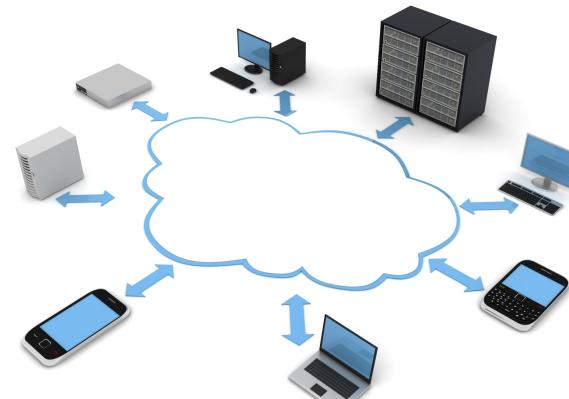
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Policy Execution

```
b ← an initial belief
while ( true )
    action ← determine an action for b using alpha vectors
    execute the action
    read observations from sensors
    update b using observations and the action
end
```

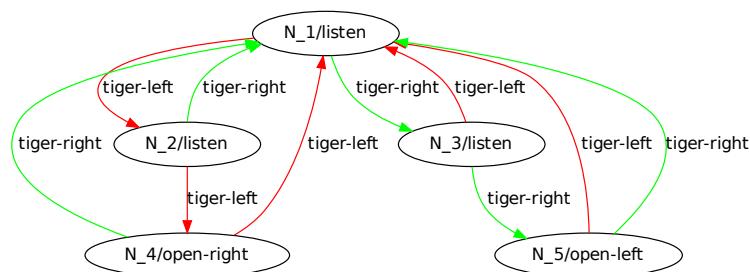
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Policy Execution in the Cloud



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Finite State Controllers



NB: No need to do a belief update nor to consult alpha-vectors.

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Battery Efficiency Experiment

- ▶ A POMDP, lacasa4.batt, with 2880 states, 72 observations, and 6 actions (engineered using WEB-SNAP¹)
- ▶ Installed on a smart phone to assist a cognitively disabled person; allows the patient enjoy her walk, helps find way home when lost, or calls a care giver when necessary
- ▶ When the patient is lost and the phone runs out of battery, the application is not available
- ▶ Relying on cloud computing requires a reliable network connection and server infrastructure

¹<https://bitbucket.org/mgrzes/web-snap>
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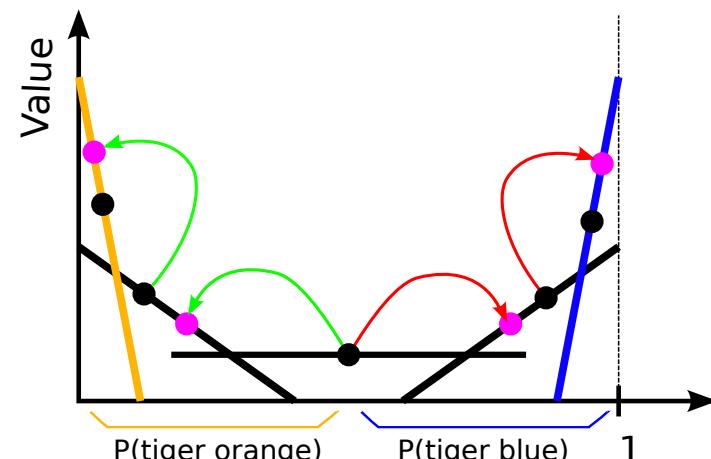
Battery Efficiency on the Nexus 4 Phone

| Experiment | 1% battery depletion time (minutes) | standard error |
|-----------------------|-------------------------------------|----------------|
| OS only | 6.74 | 0.13 |
| OS with WIFI | 6.69 | 0.08 |
| Observation generator | 6.40 | 0.26 |
| Constant policy | 5.82 | 0.21 |
| FSC | 5.71 | 0.18 |
| Client/Server (cloud) | 5.52 | 0.22 |
| Flat policy | 4.10 | 0.11 |
| Symbolic Perseus | 3.91 | 0.15 |

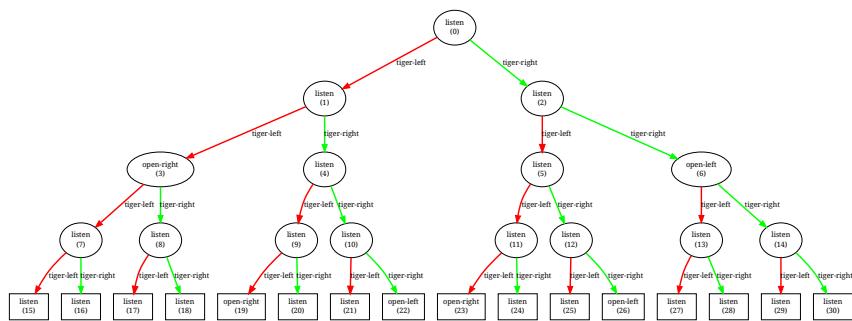
Policies for lacasa4.batt evaluated on the Nexus 4 phone. Every policy was queried once per second (time interval 1 second).

Thanks to Xiao Yang for help with running the battery consumption experiment on the phone.

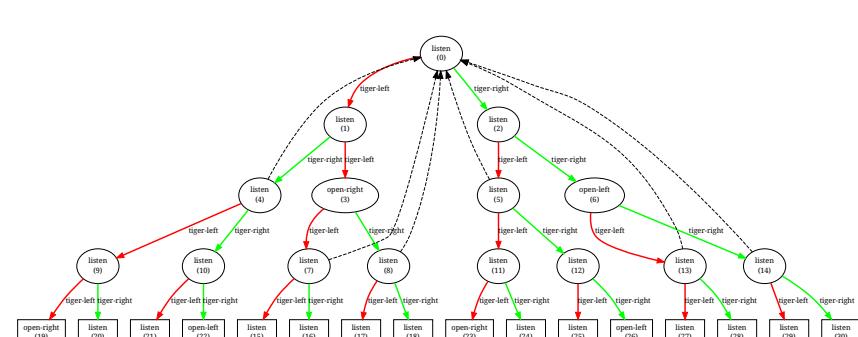
Controller Compilation Using Alpha Vectors



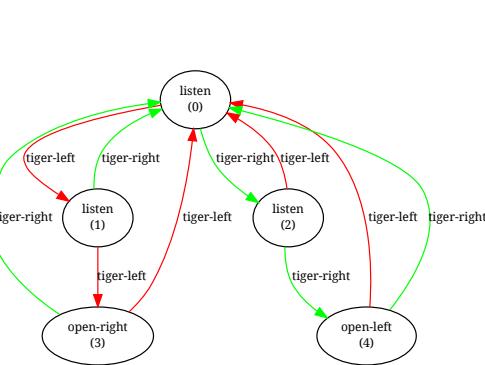
Controller Compilation Using Policy Trees: (1) Policy Tree



Controller Compilation Using Policy Trees: (2) Identical Conditional Plans



Controller Compilation Using Policy Trees: (3) Removing Repeated Nodes



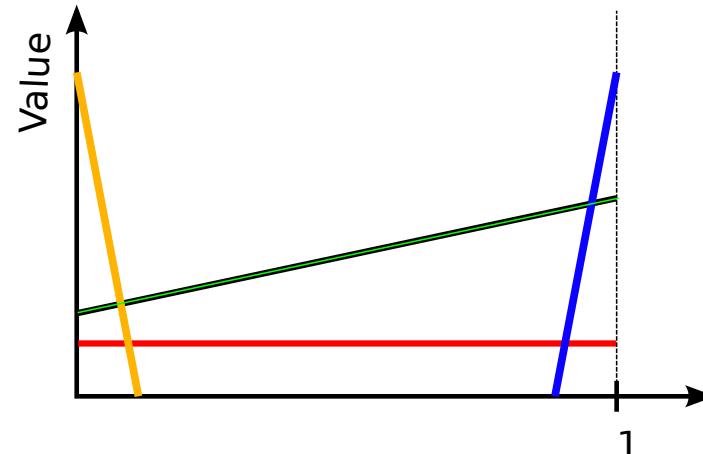
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Controller Compilation Results (1)

| POMDP | GapMin | method | depth | tree size | nodes | value | time | c |
|--|--|---|----------------|----------------|----------------------------|---|-------------------------------|-------------|
| chainOfChains3 S =10, A =4 O =1, $\gamma = 0.95$ | GM-lb=157 GM-ub=157 time=0.86s | alpha2fsc GM-LB GM-UB | 10 11 11 | 10 11 11 | 10(10) 10(10) 10(10) | 157(157) 157(157) 157(157) | 0.26 0.42 0.26 | 0 0 0 |
| | lb =10 ub =1 | B&B EM QCLP BPI | | | 10 10 10 10 | 157 0.17 ± 0.06 0 ± 0 25.7 ± 0.77 | 1.69 6.9 0.16 4.25 | |
| cheese-taxi S =34, A =7 O =10, $\gamma = 0.95$ | GM-lb=2.481 GM-ub=2.481 time=1.88s | alpha2fsc GM-LB GM-UB | 15 15 | 167 167 | 17(22) 17(24) 17(24) | 2.476(2.476) 2.476(2.476) 2.476(2.476) | 0.29 0.56 0.55 | 1 1 1 |
| | lb =22 ub =13 | B&B EM QCLP BPI | | | 10 17 17 16 | -19.9° -12.16 ± 2.08 -18.22 ± 1.77 -18.1 ± 0.39 | 24h 337.9 227.4 7.18 | |
| lacasa4.batt S =2880, A =6 O =72, $\gamma = 0.95$ | GM-lb=291.1 GM-ub=292.6 time=8454s | alpha2fsc GM-LB GM-UB | | 745 23209 | 10(10) 19(22) 87(94) | 285.5(285.5) 287.3(287.1) 290.8(290.8) | 302 3652 3681 | 0 1 1 |
| | lb =10 ub =23 | B&B EM BPI | | | 10 3 6 | 285.0° 290.2 ± 0.0 290.6 ± 0.2 | 24h 19920 4124 | |
| machine S =256, A =4 O =16, $\gamma = 0.99$ | GM-lb=62.38 GM-ub=66.32 time=3784s | alpha2fsc GM-LB GM-UB | 9 12 | 376 2864 | 5(39) 26(41) 11(159) | 54.61(54.09) 62.92(62.84) 63.02(60.29) | 5.53 18.5 86.8 | 1 1 2 |
| | lb =39 ub =243 | B&B EM QCLP BPI | | | 6 11 11 10 | 62.6 62.93 ± 0.03 62.45 ± 0.22 35.7 ± 0.52 | 52100 1757 4636 2.14 | |

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Controller Compilation: More Pruning of Redundant Nodes



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Controller Compilation Results (2)

| POMDP | SARSOP | method | depth | tree size | nodes | value | time | c |
|--|--|--|-------|-----------|-------------------------------|---|---------------------------------------|---|
| baseball $ S =7681$, $ A =6$ $ O =9$, $\gamma = 0.999$ | time 122.7s $ \alpha =1415$ UB=0.642 LB=0.641 | policy2fsc B&B EM BPI | 7 | 175985 | 10(47) 5 2 9 | 0.641(0.641) 0.636* 0.636 \pm 0.0 0.636 \pm 0.0 | 78.22 24h 48656 445 | 1 |
| elevators.inst.pomdp_1 $ S =8192$, $ A =5$ $ O =32$, $\gamma = 0.99$ | time 11,228s $ \alpha =78035$ UB=-44.31 LB=-44.32 | policy2fsc B&B | 11 | 419 | 20(24) 10 | -44.41(-44.41) -149.0* | 1357 24h | 1 |
| tagAvoid $ S =870$, $ A =5$ $ O =103$, $\gamma = 0.95$ | time 10.073s $ \alpha =20326$ UB=-3.42 LB=-6.09 | policy2fsc B&B EM QCLP BPI | 28 | 7678 | 91(712) 10 9 2 88 | -6.04(-6.04) -19.9* -6.81 \pm 0.12 -19.99 \pm 0.0 -12.42 \pm 0.13 | 582.2 24h 19295 12.9 1808 | 1 |
| underwaterNav $ S =2653$, $ A =6$ $ O =1303$, $\gamma = 0.95$ | time 10,222s $ \alpha =26331$ UB=-753.8 LB=-742.7 | policy2fsc B&B EM BPI | 51 | 1242 | 52(146) 10 5 49 | 745.3(745.3) 747.0* 749.9 \pm 0.02 748.6 \pm 0.24 | 5308 24h 31611 14758 | 1 |
| rockSample-7.8 $ S =12545$, $ A =13$ $ O =2$, $\gamma = 0.95$ | time 10,629s $ \alpha =12561$ UB=-24.22 LB=-21.50 | policy2fsc B&B BPI | 31 | 2237 | 204(224) 10 5 | 21.58(21.58)* 11.9* 7.35 \pm 0.0 | 1291 24h 78.8 | 1 |

Table: Compilation and compression of SARSOP policies.

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Conclusion

- Execution of POMDP policies on mobile devices can be battery consuming
 - Finite-state controllers are computationally cheap to execute
 - Two methods to compile POMDP policies into finite-state controllers were shown
 - Compilation is more robust against local optima than direct optimization with local search
 - Compilation is feasible on large problems where exhaustive search with branch-and-bound can be challenging