Java Threads in the Light of occam/CSP

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Abstract. Java provides support for parallel computing through a model that is built into the language itself. However, the designers of Java chose to be fairly conservative and settled for the concepts of threads and monitors. Monitors were developed by Tony Hoare (and others) in the early 1970s as a structured way of using semaphores to control access to shared resources. Hoare moved away from this, in the late 1970s, to develop the theory of Communicating Sequential Processes (CSP). One reason was that the semantics of monitors are not WYSIWYG, so that designing robust parallel algorithms at this level is seriously hard. This tutorial will look at how this impacts on threaded applications written in Java.

Fortunately, it is possible to introduce the CSP model into Java through sets of classes implemented on top of its monitor support. By restricting interaction between active Java objects to CSP synchronisation primitives, Java thread semantics become compositional and systems with arbitrary levels of complexity become possible. Multi-threaded Web applets and distributed applications become simpler to design and implement, race hazards never occur, difficulties such as starvation, deadlock and livelock are easier to confront and overcome, and performance is no worse than that obtained from directly using the raw monitor primitives.

The advantages of teaching parallelism in Java purely through the CSP class libraries will be discussed. These libraries were developed jointly at Kent and Oxford Universities in the U.K. and the University of Twente in the Netherlands.

This paper was developed from material first presented at the Java Threads Workshop [1]. It presents the basic threads model of Java, discusses why they may be a good thing but why they need special care in their management, runs through the monitor mechanisms provided in Java for their control and points out weaknesses in that control. Finally, the CSP primitives are introduced and the case for ignoring the monitor methods presented.

This work is one of the foundation stones of the JavaPP project [2], which spun out from the above workshop. The other founding stones [3, 4, 5, 6] were first presented at the WoTUG-20 conference last year.

1 The world is parallel – enjoy

1.1 Concurrency is everywhere

The natural world is certainly not organised through a central thread of control. Things happen as the result of the actions and interactions of (unimaginably) large numbers of independent agents, operating at all levels of scale from nuclear to astronomic. Computer systems aiming to be of real use in this real world need to model, at the appropriate level of abstraction, that part of it for which it is to be of service. If that modelling can reflect the natural concurrency in the system, it ought to be much simpler.

Yet, traditionally, concurrent programming is considered to be an advanced and difficult topic – certainly much harder than serial computing which, therefore, needs to be mastered first. But this tradition is wrong.
Java recognises this, a little bit, by binding some notions of concurrency into the language, rather than leaving it to semantic-busting changes introduced through some external library. We will quarrel with the antiquity and semantic imprecision (so far) of some aspects of the Java thread primitives, but at least they give us a platform on which something sound and easy-to-use can be built.

Java threads are not exactly highlighted in the current range of books. It is easy to get the impression that they are a somewhat exotic feature with only a narrow field of application. Warnings are frequently given as to the difficulties in their safe use – we are advised to use them only when we absolutely can’t get away with not using them! This does not square with our view that concurrency is a powerful abstraction that simplifies the design and implementation of systems, to be used every day on a broad field of application.

1.2 Threads: problems and opportunities

A ‘normal’ program has a single thread of control. Instructions execute one at a time in the order written in the code and dependent upon the state of the data being processed. A ‘concurrent’ program has many threads of control whose instruction sequences proceed ‘simultaneously’. Each thread may be executed by a different processor (e.g. on an SMP platform) and each processor may have a different speed. More commonly, all the threads may be scheduled on a single processor, with their individual flows of logic arbitrarily interleaved. Either way, no assumptions can be made about the relative rates of progress of individual threads.

Threads also live in a shared memory space. They may declare and manipulate their own data and, optionally, make them available to other threads (although this is not usually a good idea). They may also operate on shared (external) data structures. In which case, some rules for coordinating access need to be designed and enforced if chaos is to be avoided. For example, it is not a good idea to allow two threads to update the same piece of data at the same time.

There are many ways to arrange this coordination, but all of them expose new dangers. For example, a group of threads may get into a state where each one is waiting for another to do something that will enable it to proceed – DEADLOCK! Or a group of threads may get into an infinite cycle of interaction amongst themselves and refuse to respond to anything outside their group – Livelock! Or a thread may get blocked forever, waiting for a condition that the other threads never set up for it – Starvation! And if we avoid all this, we can still get the coordination wrong and, intermittently, allow uncontrolled access to some shared resource and get unpredictable system corruption – Race Hazard!

On the other hand, if we can master these problems, systems do become simpler – with benefits across the whole engineering life-cycle. We can also achieve significant gains in performance and responsiveness through the direct targeting of parallel hardware. These include not only shared-memory (or virtual shared-memory) multi-processors, but also parallel use of a single processor (for computation) with communication hardware (e.g. for Internet links).

Of course, no performance benefits will arise if the overheads of multi-threading (e.g. for coordination and context switching) swamp the processing the user actually wants the system to do. The faster our processors become, the lower must be these overheads. In 1987, the T800 transputer was the fastest microprocessor in the world, with a one microsecond floating-point time and a one microsecond (hardware assisted) context switch. In 1997, processors can be hundreds of times faster at floating-point, but fifty times slower at context-switching – even with ‘lightweight’ threads mechanisms! Something has gone wrong.
1.3 Some objects are more oriented than others

There is a superficial resemblance between the concepts of object (as provided by O-O languages such as Java) and process (as given by the occam/CSP model[7, 8, 9, 10, 11, 12]). Both concepts encapsulate data structures and the algorithms to manage those data structures – but:

- in occam/CSP, the algorithms form an autonomous thread of control that directly expresses the behaviour of the object from its own point of view;

- in Java (and most other O-O languages), the algorithms implement ‘methods’ which need to be invoked by some external agent (another object). This invocation forms part of that external agent’s thread of control. The algorithms express the behaviour of their object from the point of view of the calling agent.

So, we reach the curious conclusion that, until the concepts of thread and object are bound together, object algorithms are not really object-oriented in the natural language sense of the term, but are caller-oriented – in the same way that procedures, in a traditional language such as Pascal, are caller-oriented.

1.4 Get a life

The magic ingredient that gives us the useful paradigm shift is the thread. In occam/CSP, this is automatic – processes are live objects executing their own logic via their own threads of control. In Java, if we want to give life to our objects, we have to do some extra work to set this up – but, at least, it can be done and it’s not really that hard.

1.5 Living together

However, a system cannot just consist of active objects. They need to interact as they collaborate to get their overall job done. They can’t simply call each other’s methods to determine and/or alter each other’s state – that leads to race hazards and unpredictable behaviour. Some ways to coordinate these interactions need to be found.

In occam/CSP, processes interact with each other via channels. Channels are passive objects – they have no life of their own and are just there to be used by the processes they connect. They provide a communication mechanism between processes that is synchronised.

A process may write to a channel at any time, but has to wait for some other process to read from that channel before it can continue. Similarly, a process may read from a channel at any time, but has to wait for another process to write before it can continue. Whoever gets to the channel first – the writing process or the reading one – is blocked. Blocking is entirely passive, the blocked process consuming no processor time.

Note that a channel is used just for synchronisation and does not buffer transit data itself. A good implementation will cause the data (or, possibly, a reference to the data) to be transferred directly from the writing to the reading process. Channels may be 1-1 (private line), many-1 (multiplexing), 1-many (de-multiplexing) or many-many (public exchange).

Notice also that it is entirely up to the process whether it chooses to read or write from a channel. For example, if some server process has run out of a crucial ingredient it needs to provide its service, it just doesn’t read from the channel along which requests arrive. This leaves clients neatly and passively queued on the request channel, from which they can easily be retrieved (once the missing ingredient has been replenished) simply by performing the necessary reads.
In Java, we don’t have channel primitives but we have plenty of passive objects – these are ‘normal’ objects that do not contain any threads. Happily, Java provides enough synchronisation mechanisms to allow us to build channels out of passive objects. We have done this – but it was not easy ...

1.6 The trouble with monitors

The Java threads model is (somewhat loosely) based upon the concepts of monitors and condition-variables. These were developed in the early 1970s (by Dijkstra, Brinch-Hansen, Hoare and others) as a structured way of using the more primitive notions of semaphores. The standard reference quoted by Sun is [13].

Nevertheless, monitors and condition-variables are not easy to use. Their semantics are volatile and do not compose. Individual methods have to be sensitive to the behaviour of their siblings, upon which they rely to establish conditions that will allow them to proceed if they get stalled. To write and understand one (synchronised) method, we need to write and understand all the (synchronised) methods at the same time – we can’t knock them off one by one! To develop $n$ methods, we need to consider $O(2^n)$ possible interactions. This type of logic does not scale and is not for everyday work.

In the late 1970s, Hoare broke entirely new ground with CSP. Some authoritative sources claim that Java threads are based upon CSP, but this is plainly wrong. Would that it were true! CSP semantics are denotational – a mathematical term for WYSIWYG. As we have noted, CSP processes can refuse individual events if they are not in a state to accept them. Each process has its own contract and looks after itself. This type of logic does scale – we don’t have to understand the whole in order to understand the part. The whole is the orthogonal composition of the parts.

2 Synchronising parallel threads – the Java primitives

A thread starts, runs for a while (possibly forever) and then finishes. Whilst it is running, it may get blocked for various reasons. Sometimes this is voluntary – for example, it may just choose to sleep for some period (to allow other threads a greater share of the processor or simply because its next actions aren’t yet due). Sometimes this is forced – because a resource that it needs (like some user input or buffer space or some data being calculated by another thread) is not yet available.

Some texts distinguish between two types of ‘running’ threads: those that are actually being executed (on a uni-processor, there will be just one of those at any one time) and those that are able to run but are waiting their turn for the processor (normally there will be many more threads than processors and the interleaving of runnable threads on any processor is managed by the underlying threads kernel). However, systems should be designed that are independent of this underlying scheduling, so we make no such distinction.

This tutorial is about ideas (semantics) rather than detailed syntax. For a formal presentation of the Java thread primitives, see one of the many textbooks (such as [14]). We assume a little familiarity with the Java syntax for classes, methods and flow-control, but will generally be fairly relaxed.

2.1 Basic threads in Java

A thread is created when we declare an instance of a class extending the built-in Java class Thread. For instance:
class Thing extends Thread {
    ... attributes
    ... constructor method(s)
    public void run () {
        ... do things
        suspend ();
        ... do some more things
    }
}

If we now declare an instance:

    Thing T = new Thing ();

the run method of T will start to run, logically in parallel with the thread that has just declared it. Given the way it has been programmed, the newly spawned thread will do some things and then, voluntarily, suspend itself. If no other thread does anything to resume it, it will stay in that blocked state forever.

Suppose the spawning thread were programmed:

    Thing T = new Thing (); // T starts to run
    ... do our own stuff
    T.resume (); // kick T back to life (maybe)
    ... carry on // is T running again?

After spawning thread T, we spend some time doing ‘our own stuff’ and, then, execute T.resume. There are two possibilities: either T has reached and executed its suspend instruction (in which case, it will be properly resumed) or it has not (in which case, nothing happens). In the latter case, T will eventually suspend itself. The problem is that, in our code marked ‘carry on’, we have no idea whether the thread T is running or not – presumably, we wanted it to be running! This is an example of a race hazard: the state of the system is not being controlled by us but by the rates of progression of the various threads (over which we do not have absolute control).

If we know something about the scheduling of the spawning and spawned threads, and about the relative timings of their ‘do things’ and ‘do our own stuff’ code fragments, we might be able to deduce that the suspend happened before the resume and that all is well. If the timings worked out wrong, we could try to fix things by:

    Thing T = new Thing (); // T starts to run
    ... do our own stuff
    sleep (2*seconds);
    T.resume (); // kick T back to life (maybe)
    ... carry on // is T running again?

but this is desperate stuff! The problem is that there is no notion of synchronisation built into the suspend and resume thread methods and, without it, we can’t keep control of what’s going on in a way that is robust and independent of the underlying threads management. We don’t recommend the use of suspend/resume.

[Aside: there is another way to create a thread in Java. If we want an object to run a thread and extend some other class, we can’t proceed as above. Java does not allow multiple inheritance – we can’t extend from both the Thread class and some other one. To get around this, we extend from that other class and say that our extended class also implements an interface called Runnable. Interfaces just contain method headers and Runnable just contains the run header. We define a run method inside our extended class and declare and start up a raw Thread object so that it uses our own run method. The information in this tutorial is independent of whichever way of creating threads is used.]
2.2 Another reason to synchronise

Suppose we have a simple Counter class:

```java
class Counter {
    private long count = 42;
    public void increment () {
        count++;
    }
    public void decrement () {
        count--;
    }
    public long value () {
        return count;
    }
}
```

and a particular instance:

```java
Counter X;
```

Suppose we have two threads operating on the same X. Suppose they make calls whose interleaved sequence is indicated by:

```
. 42            .
. 42            .
. 42            .
X.increment () 43   X.increment ()
. 43            .
. 43            .
X.increment () 43
. 44            .
. 44            .
. 44            .
X.increment () 43   X.increment ()
. 45            .
. 45            .
X.decrement () 45
. 44            .
. 44            .
```

where time flows down the page, the left column indicates when the first thread invoked X-methods, the right column indicates when the second thread invoked them and the middle column traces the value of the private X.count.

Because the calls did not overlap, the state of the counter was updated correctly. However, we can’t assume the calls will never clash. Suppose the scheduling on the first thread was a little earlier:

```
. 42            .
. 42            .
X.increment () 42   X.increment ()
. 43            .
. 43            .
. 43            .
. 43            .
X.decrement () 43   X.increment ()
. 42            .
. 42            .
```
This time, the two threads attempted to increment the count at (around about) the same time. What happened is that one thread had loaded the value 42 into its processor’s registers when the processor switched context to the other thread. The second thread completed its increment operating on the 42 value still in memory, writing 43 back. Context switched back again to the first thread, which completes its interrupted increment using the 42 value it had originally loaded, and also writes 43 back into memory. Two increments happened, but the value in `X.count` only went up once.

Later, there was another clash between an increment and a decrement. In this case, the decrement was the interrupted operation, finished last and left 42 back in `X.count`. It could equally have happened the other way around, leaving a final value of 44.

These errors are also the result of race hazards due to a lack of synchronisation between the threads.

### 2.3 Monitors

Java provides a synchronisation mechanism based upon the concept of monitors. A monitor is a class whose methods can only be executed by one thread at a time. It enables atomic (i.e. safe) updating of data within the monitor by any number of threads. In Java, all we do is add one keyword to the method declarations:

```java
class Counter { // this is a monitor
    private long count = 42;
    public synchronized void increment () {
        count++;
    }
    public synchronized void decrement () {
        count--;
    }
    public synchronized long value () {
        return count;
    }
}
```

In this case, each instance of a `Counter` object has a lock which has to be acquired by any thread invoking one of its methods. Only one thread can hold this lock at any one time. So, if one thread is in the middle of `X.increment` when another thread calls `X.decrement`, the second thread will have to wait until the first call has finished.

So, with the clashing scenario that caused data corruption before, what would happen this time is:

```
  . 42
  . 42
  X.increment () 42 X.increment ()
  . 43 <block>
  . 44
  . 44
  . 44
  . 44
  X.decrement () 44 X.increment ()
  . 43 <block>
  . 44
  . 44
  . 44
```
where the first thread acquired the lock first each time and the second one had to wait. But the \texttt{X.count} would have been securely updated whichever thread had won the race – there is no hazard. So far so good!

One final point about Java’s monitors: what happens when there are lots of threads vying for the lock at the same time? The Java language definition is imprecise here. What happens is left to the threads management kernel that underlies the Java Virtual Machine (JVM). In all implementations I’ve seen, the threads form an orderly queue for the lock. In that case, so long as no method executes forever and so long as no deadlock occurs, each thread is bound to reach the front of that queue and invoke the method on the monitor – no starvation here. However, we should note that this simple and fair mechanism is not guaranteed by the Java language.

2.4 Conditions

Sometimes we queue up for something only to find, when we finally get served, that they’ve run out of the particular item we wanted! Well, we can always go away and try again later. But that gives no guarantee that we’ll ever get back at the right time to find what we wanted – a danger of livelock and starvation.

Some shops provide a stand-by area where we can wait if the item we want isn’t available. When a delivery arrives, we can be notified to come and get it.

These stand-by areas are called condition variables in monitor theory. Hoare’s paper allowed for as many (named) condition variables as the designer of the monitor wanted, but Java allows only one.

There is another weakness arising from the current imprecision of Java’s semantics. Hoare specifies that, when a waiting thread is notified, it immediately acquires control of the monitor lock and resumes execution. This is only reasonable, since the reason it is notified is that the condition for which it was waiting has been established – it needs to be able to exploit that. Otherwise there was not much point in the notification!

But there is no such immediacy mandated for Java. In fact, current systems send the notified thread from the stand-by area to the back of the queue for the lock – a queue it has already been through once! By the time it gets back to the front of this queue, the condition which triggered its notification may no longer apply. As we shall see, this causes trouble.

Java provides three forms of waiting and two kinds of notification. They can only be invoked once the calling thread is in possession of the monitor lock for that object (e.g. inside a synchronized method for that object):

- **wait ()**
  The calling thread is blocked and the monitor lock is released. If there are several threads that get blocked like this for the same object, Java does not say how they are managed. Current implementations hold them in a queue, but it may not be safe to rely on this. When some other thread invokes a notify method on this object, one of the waiting threads is released. Again, this is normally the thread that has been waiting the longest. The released thread ought to be immediately given the monitor lock, so it can take advantage of the condition set up by the releasing thread. Current implementations put it to the back of the queue of threads trying to acquire the monitor and let the notifying thread retain the lock and carry on.

- **wait (long timeout)**
  This is the same as the above, except that after timeout milliseconds without release-by-notification, the thread is released anyway (to the back of the monitor queue).
- **wait** (long timeout, int titch)
  This is the same as the above, except that the timeout period is timeout milliseconds plus titch nanoseconds. The value of titch should be in the range 0 through 999999.

- **notify ()**
  This releases one of the waiting threads – see the remarks for wait above. If there are no waiting threads, nothing happens.

- **notifyAll ()**
  This releases all the waiting threads (if any).
  [Aside: this method is not envisaged in Hoare’s paper on monitors [13]. It somewhat clobbers the key property that Hoare had specified that notified threads immediately take over the monitor lock and resume execution – they can’t all do that! Including this method may be the reason Java does not mandate this property for the ordinary notify method.]

### 2.5 Example: a simple FIFO buffer

Consider a passive object that provides FIFO buffering between active writer threads and active reader threads. Its top-level structure is:

```java
class Buffer {
    private final int max = 100; // buffer size
    private int[] buffer = new int[max]; // space to hold the buffered data
    private int size = 0; // number of items currently held
    private int lo = 0; // index of oldest item in the buffer
    private int hi = 0; // index of next free slot in the buffer

    public synchronized int read () {...}
    public synchronized void write (int n) {...}
}
```

This is a simple integer buffer with a fixed size (100). It could easily be modified to buffer arbitrary Objects and have a user-chosen size, but that’s not relevant to our problem.

The private data structures are guaranteed atomic update by the synchronized methods that operate on them. But what happens when a reader thread acquires the monitor lock and finds the buffer is empty? Rather than giving up and exiting, the reader can wait in the stand-by area:

```java
public synchronized int read () throws InterruptedException {
    int index;
    if (size == 0) wait (); // hopefully, size is now greater than zero :-)
    size--;
    index = lo;
    lo = (lo + 1) % max;
    return buffer[index];
}
```
[Aside: just ignore the throws InterruptedException stuff! This exception may be thrown by the wait method we are about to use. Rather than handle this here, we are throwing it back to the thread that called this read (who may know something sensible to do with it!)]

Executing the wait releases the monitor lock and this thread becomes blocked. Any other reader threads invoking this read method will similarly be put on hold. Hopefully, a writer thread will come along, put something into the buffer, increment the size, update the hi pointer and issue a notify.

Issuing a notify causes one of the waiting reader threads to move out of the stand-by area and resume execution. However, first it has to re-acquire the monitor lock ... and current implementations make it queue up again! If it finds itself behind another reader and behind no other writers, by the time it gets back the buffer will be empty again.

Consequently, Java authorities (such as [14]) tell us never to wait for a condition using an if, but to use a while:

```java
public synchronized int read () throws InterruptedException {
    int index;
    while (size == 0) wait ();
    // if we ever exit the above, size *will* be greater than zero :-)
    size--;
    index = lo;
    lo = (lo + 1) % max;
    return buffer[index];
}
```

The problem with the above is proving we will ever exit the while-loop. If there is only one reading thread, we will go round at most once. But if there are more than one, we have no guarantees and just have to hope for the best!

There are other problems. Viewing the above method in isolation, it makes no sense. The semantics of the given while-loop implies no exit, since nothing happens in the loop body to alter the while-condition. Of course, we can’t reason about this method in isolation – it depends intimately on its sibling write method:

```java
public synchronized void write (int n) throws InterruptedException {
    while (size == max) wait ();
    // if we ever exit the above, there *will* be room in the buffer :-) 
    buffer[hi] = n;
    hi = (hi + 1) % max;
    size++; // implies size > 0
    notify (); // in case there is a waiting reader
}
```

Executing the notify method summons one of the waiting reader threads out from the stand-by area. If there were no waiting threads, nothing happens – the unnecessary call is said to be benign. Notice that we issue the notify immediately after doing something that ensures that the condition being waited for (in this case, that size is non-zero) has been established.

Note also that a writer thread, having acquired the monitor lock, will also have to wait if the buffer is full. This means that we need to go back to the read method and get it to issue a notify in case there was a waiting writer:
public synchronized int read () throws InterruptedException {
    int index;
    while (size == 0) wait ();
    // if we ever exit the above, size *will* be greater than zero :-)
    index = lo;
    lo = (lo + 1) % max;
    size--; // implies size < max
    notify (); // in case there is a waiting writer
    return buffer[index];
}

[Aside: a simpler (one-place) version of this Buffer class is given in Sun’s on-line tutorial [15]. Their class is called CubbyHole and is programmed in an identical style to the version of our Buffer we have reached so far. And it has the same deficiencies.]

    The continual juggling between the two methods to get their mutually dependent semantics correct is not good news – and we are not finished yet!

    When the reader issues the notify and there was a waiting writer, what ought to happen is that the reader immediately relinquishes the monitor lock to the notified writer (because the condition for which it was waiting has been set up). If that happened in this case, the notified writer would immediately fill up the last place in the buffer. Unfortunately, that would overwrite the buffer[index] this method still has to return!

    In current implementations, this doesn’t happen – the notified writer is put on the back of the monitor queue and the reader thread retains the monitor lock and carries on – in which case, the above code is OK. However, this doesn’t look like something we should rely upon! Rather than remembering the index to the item we are supposed to be reading, we had better save the whole thing:

    public synchronized int read () throws InterruptedException {
        int save;
        while (size == 0) wait ();
        // if we ever exit the above, size *will* be greater than zero :-)
        save = buffer[lo];
        lo = (lo + 1) % max;
        size--; // implies size < max
        notify (); // in case there is a waiting writer
        return save;
    }

    The save variable is local to this method and will be a different variable for each invoking (but stalled) thread. That fixes that.

    However, there is one last thing that is unsatisfactory about the above code. I really don’t like the calling of notify when there are no waiting threads. It’s not just the unnecessary overhead – it’s the lack of synchronisation involved (a bit like the way resume works on threads that have not executed a suspend). Such sloppiness will lead to trouble in the long run.

    In this case, the sloppiness can be removed by maintaining private counts (inside the Buffer object) of the number of waiting readers and writers. These could be incremented just before executing a wait and decremented just before executing a notify. The nice thing is that the call to the notify can then be made dependent on whether there is any waiting thread. This is left as an exercise.

    Reminder: the livelock/starvation problems associated with completing the while-loops that are waiting for the conditions (in the case of multiple readers and writers) have not yet been addressed.
2.6 *Wot, no chickens?*

This example illustrates the danger of simply waiting for a condition in a `while`-loop when there are multiple consumers of that condition. It is described in detail in [1] and outlined here.

A college consists of five philosophers, a chef and a canteen – see Figure 1. The chef and the philosophers are *active* objects. The canteen is a *passive* object through which the philosophers and the chef interact. The canteen is implemented in the style of the above `Buffer` class (and Sun’s `CubbyHole`).

![Diagram of philosophers and canteen](image)

**Figure 1: The greedy but starving philosopher**

The philosophers think for a while and then go to the canteen for food. Except for one of them ... who is plain greedy, never thinks and just keeps going to the canteen.

The chef cooks in batches of four, replenishing the canteen when each batch is ready. The greedy philosopher always misses out! He gets there too early the first time (no food yet) and is put on hold. When released, he is put on the back of the canteen queue again ... behind his colleagues who arrived whilst he was on hold. His colleagues take the whole batch just arrived from the kitchen and he gets put on hold again. He never gets out of this cycle.

This infinite starvation and livelock does depend on bad luck with the timing. But that is typical of race hazards and we cannot rely on good luck in order to be safe. The timings are as follows:

- the philosophers and the chef start up around the same time;
- philosopher 0 thinks for no time at all;
- the other philosophers think for 3 seconds before going to eat;
- the chef cooks chickens in batches of 4 and takes 2 seconds per batch. Delivery to the canteen takes around 3 seconds (the chickens are hot!) and the chef helps to set them down. During this time, the canteen cannot accept further orders from philosophers (who will have to queue) because its lock is owned by the chef.

What happens is:

- **second 0**: the system starts up. Philosopher 0 calls `Canteen.get` and is made to wait since there are no chickens yet. The chef starts cooking and the other philosophers start thinking.
second 2: the chef calls on Canteen.put with 4 chickens. Setting them down is going to lock up the canteen for the next 3 seconds.

second 3: the other 4 philosophers try to call Canteen.get, but cannot acquire its monitor and have to get in line.

second 5: the chef finally sets down the batch of 4 chickens and calls notifyAll to release anyone waiting. In this case, it's just philosopher 0 and he has to go to the back of the line.

The chef exits the Canteen.put method which allows the philosophers to make their Canteen.get calls. Philosophers 1 through 4 go through in sequence, taking all the chickens. Finally, philosopher 0 makes the call and is put on hold again.

The chef starts cooking again and the other philosophers start thinking. We are back to the state we were in at second 0 and everything repeats – forever! Greedy philosopher 0, despite being always first to the canteen, never gets served.

Here is the code for the Canteen:

class Canteen {
    private int n_chickens = 0;
    public synchronized int get (int id) throws InterruptedException {
        while (n_chickens == 0) {
            ... complain ("Phil " + id + ": Wot, no chickens?")
            wait();
        }
        ... place order ("Phil " + id + ": Those chickens look good ...")
        n_chickens--;
        return 1;
    }
    public synchronized void put (int value) throws InterruptedException {
        ... shout ("Chef : Make room ... this dish is very hot ...")
        Thread.sleep (3000); // take 3 seconds to set down the dish
        n_chickens += value;
        ... announce ("Chef : More chickens ... NOTIFYING ...")
        notifyAll (); // wake up any waiting philosophers
    }
}

where the dotted lines indicate some print statements for animating what's happening.

This code follows the same style as Sun's CubbyHole and gives little indication of the danger to which its callers are exposed. We've used notifyAll rather than notify, but it makes no difference in the scenario we have set up – there is only ever one thread waiting for the chickens (philosopher 0).

What is the matter with this design? Clearly, the chef should not have to queue up with the philosophers to get into the canteen. The philosophers should have their own queue and the chef should only have to contend with one philosopher when dealing with the chickens in the canteen. However, we are modelling this Canteen on the CubbyHole class (to show the danger of starvation it contains) and CubbyHole has its queue shared by both readers and writers.

A more serious complaint – from the point of view of object-orientation – is as follows. All methods, apart from a run method, are executed as part of the thread of control of their calling objects. This is particularly clear here, where we see them speaking as those calling objects. For instance, the Canteen.get method is part of the life of the calling
philosopher and \texttt{Canteen\_put} is part of the life of the chef. So, this canteen object has bits of philosopher-algorithm and bits of chef-algorithm for its methods – a somewhat confused set of roles for something that’s supposed to be a canteen. There’s nothing in these methods that are oriented towards the life of the canteen.

These problems are not special to this \texttt{Canteen}, but are universal across all passive objects.

The canteen should, of course, be implemented as an active object connected to the philosophers and the chef via simple channels. Then, we wouldn’t have the problems arising from this design. This comes next!

3 Synchronising parallel threads – the JavaPP primitives

This section introduces the basic JavaPP (i.e. occam/CSP) synchronisation primitives. These can be used exclusively to provide the glue to coordinate and exchange information between active threads – we never need to get involved again with \texttt{synchronized} methods or \texttt{wait} and \texttt{notify}.

Armed with them, multi-threaded code becomes \textbf{WYSIWYG} and system complexity can be ramped up with linear increase in effort. No run-time overheads are imposed that wouldn’t be needed anyway to prevent race hazards. We can inherit the rich treasury of occam/CSP design and analysis methods/tools. Multi-threaded systems can be structured to reflect real world system hierarchies. Components become automatically thread-safe and reusable and the nasty accidents of deadlock, livelock and starvation can be ruled out by design.

But first we have to implement the primitives. These will be passive objects in the normal sense and we will have to do the hard work – \textit{one last time} – of safely using the raw Java monitors.

3.1 Channels : review

\textit{Channels} were described in Section 1.5. They provide synchronised (un-buffered) communication between a pair of threads – except that, from now on, we are going to refer to threads as \textit{processes} (out of deference to CSP).

Recapping what was said earlier, a process may write to a channel at any time, but has to wait for some other process to read from that channel before it can continue. Similarly, a process may read from a channel at any time, but has to wait for another process to write before it can continue. Whoever gets to the channel first – the writing process or the reading one – is \textit{blocked}. Blocking is entirely passive, the blocked process consuming no processor time.

3.2 Channels : first attempt

For the moment, we are going to restrict ourselves to a channel that only allows integers to be communicated – extending this to carry arbitrary objects is trivial. We also restrict the channel to support only a \textit{single} reader and a \textit{single} writer. It was \textit{multiple} readers and writers that gave rise to the race hazard that caused infinite starvation when using the \texttt{Buffer} class above. We shall postpone solving that problem for a short while.

Here is a first attempt at the channel. The top-level structure is:
class Channel {
    private int channel_hold;
    private boolean channel_empty = true; // synchronisation flag
    public synchronized int read () throws InterruptedException {...}
    public synchronized void write (int n) throws InterruptedException {...}
}

The channel Hold attribute holds the value of the data being communicated through the channel. This is transient and the users of the channel cannot detect that it is buffered here temporarily. [Aside: for a channel carrying objects, channel Hold will just contain a reference to the object being transmitted.]

The channel Empty flag records whether the channel has a (reader or writer) process waiting on it.

The methods are short and sweet – but kind of tricky:

    public synchronized int read () throws InterruptedException {
        if (channel_empty) {
            channel_empty = false; // first to the rendezvous
            wait (); // wait for the writer process
        } else {
            channel_empty = true; // second to the rendezvous
            notify (); // schedule the waiting writer
        }
        return channel_hold;
    }

So, if the reader is first to the channel, it sets the flag and waits. It will be released later by the writer process (see below), which has first cleared the flag and written into channel Hold. Once released, all the reader has to do is return this value.

If the reader is second to the channel, the writer has already written into channel Hold and set the synchronisation flag. We clear the flag, notify the writer to be released and return the value that has been written.

Nearly-but-not-quite symmetrically, the writer is implemented:

    public synchronized void write (int n) throws InterruptedException {
        channel_hold = n;
        if (channel_empty) {
            channel_empty = false; // first to the rendezvous
            wait (); // wait for the reader process
        } else {
            channel_empty = true; // second to the rendezvous
            notify (); // schedule the waiting reader
        }
    }

The writer can always write, straightaway, into channel Hold – it doesn’t matter whether the reader got there first or not.

Next, if the writer is first to the channel, it sets the flag and waits. It will be released later by the reader process (see above), which first clears the synchronisation flag. Once released, all the writer has to do is exit.

If the writer is second to the channel, then the reader is waiting. We clear the synchronisation flag, notify the reader to be released and exit.
3.3 Channels: paranoia

The above seems to work for current implementations ... but we ought to be careful. There is a potential danger in the reader code. In the case that it was first to the rendezvous and waiting, what does the writer process do after notifying the reader? Well, it exits and could immediately have something else to write down this channel and issue another write. If by any chance that second write got in the queue to the channel monitor before the reader it just notified, the data from the first write – which the reader still has to return – will be lost! This is an unlikely, but possible, way that the underlying threads mechanism may chose to schedule these things. It would be nice if we could rule it out.

There is a similar danger if the reader was second to the rendezvous and has to notify the waiting writer. For the moment, invoking notify does not seem to hand over the monitor lock to the process being notified (so that it can exploit the condition that caused us to issue the notification). If it did, the notified writer would simply exit ... and we would be back with the scenario from the previous paragraph.

Let’s be paranoid and guard against all this. If the reader were second to the rendezvous, we can take another copy locally (within the read method) before notifying the waiting writer and return that local copy. If the reader were first to the rendezvous and waiting, let’s make sure it regains the monitor before the notifying writer exits its write method – we can do this simply by forcing the writer to wait after it notifies the reader. Then, it is as though the reader had been second to the rendezvous (i.e. we take a local copy, notify the waiting writer and return the local copy). The reader and writer methods become:

```java
public synchronized int read () throws InterruptedException {
    int local;
    if (channel_empty) {
        channel_empty = false;   // first to the rendezvous
        wait ();                 // wait for the writer process
        local = channel_hold;    // take a copy of what was written
        notify ();               // schedule the writer to finish
    } else { // channel_empty = true;
        channel_empty = channel_hold;  // second to the rendezvous
        notify ();                      // take a copy of what was written
        notify ();                      // schedule the waiting writer
    }
    return local;
}
```

and:

```java
public synchronized void write (int n) throws InterruptedException {
    channel_hold = n;
    if (channel_empty) {
        channel_empty = false;   // first to the rendezvous
        wait ();                 // wait for the reader process
    } else { // channel_empty = true;
        notify ();                 // second to the rendezvous
        wait ();                      // let the reader regain the lock
    }
}
```

Phew!
3.4 Channels: multiple readers and writers

We now extend the channel so as to make it secure for use by multiple readers and writers. We still want full synchronisation between a reading and writing process. Any process may read or write on this channel. Readers and writers are queued separately. A reader only completes when it gets to the front of its queue and finds a writer. A writer only completes when it gets to the front of its queue and finds a reader. There is no logical buffering of data in the channel.

Figure 2: A shared channel

Figure 2 illustrates the connection: the smiling faces are active processes and the thick arrow (plus its stubs) represents the passive object that is the shared channel.

The previous version of Channel guarded its waits with a simple if-condition. We did not need to use a while – as recommended by many textbooks – because we only had two processes to worry about (one reader and one writer). We do not want to use a while now because of the lack of guarantee that it will ever exit.

Instead, we make the readers go through their own reader-queue before trying to access the channel. We make the writers do the same on their own writer-queue. That way, we ensure that there is still only a single reader and a single writer actually competing to use the channel itself – and we can use the previous algorithm.

Every object in Java contains a monitor on which we can queue processes simply by making them synchronize on it. The simplest way to do this is to make use of another facility of Java – the synchronising block (rather than synchronising methods). To explain what this is, consider a Java monitor method:

```java
public synchronized int f () {
    ... body of the method
}
```

This is equivalent to an unsynchronised method whose body is guarded by a synchronize command on the monitor object:

```java
public int f () {
    synchronized (this) {
        ... body of the method
    }
}
```

Of course, the synchronised block need not be the whole of the body:

```java
public int g () {
    ... stuff
    synchronized (this) {
        ... exclusive execution here
    }
}
```
where only one process at a time can execute the synchronised code. We can also synchronise on any Java object, so long as we know its name, and we make use of this to construct our extended channel:

class Channel {
    private int channel_hold;
    private boolean channel_empty = true;

    Object read_monitor = new Object(); // all readers multiplex
    Object write_monitor = new Object(); // all writers multiplex

    public int read () throws InterruptedException {
        synchronized (read_monitor) { // compete with other readers
            synchronized (this) { // compete with a single writer
                int local;
                if (channel_empty) {
                    channel_empty = false; // first to the rendezvous
                    wait (); // wait for the writer thread
                    local = channel_hold; // take a copy of what was written
                    notify (); // schedule the writer to finish
                } else {
                    channel_empty = true; // second to the rendezvous
                    local = channel_hold; // take a copy of what was written
                    notify (); // schedule waiting writer thread
                }
                return local;
            }
        }
    }

    public void write (int n) throws InterruptedException {
        synchronized (write_monitor) { // compete with other writers
            synchronized (this) { // compete with a single reader
                channel_hold = n;
                if (channel_empty) {
                    channel_empty = false; // first to the rendezvous
                    wait (); // wait for the reader thread
                } else {
                    channel_empty = true; // second to the rendezvous
                    notify (); // schedule waiting reader thread
                    wait (); // let reader regain this monitor
                }
            }
        }
    }
}

The methods are the same as before except that, before synchronising on the channel monitor itself, we have to synchronise on our respective (reader or writer) monitor. It is crucial, therefore, that the methods are not synchronized themselves.
3.5 Channels: choosing between them

So far, we have only shown how to read and write on channels. Sometimes, we want to wait on a number of channels and choose the first one that becomes ready – i.e. has a process trying to use it at the other end. This implies making some declaration of intent that we are willing to use any of the channels. When we find one that is ready, we need to withdraw that declaration of intent from the others and commit to the one selected.

Allowing both sides of a channel communication to back off such a declaration is possible, but requires considerable overheads for its secure management. Although CSP allows this, we adopt the same compromise made by the occam multiprocessing language and only allow readers the luxury of backing off. This constraint significantly reduces overheads and, as found in over a decade of industrial and academic practice, does not significantly limit our freedom in design.

We also insist that when a process is waiting on a bunch of channels, no other process may be reading from any of them. In other words, such channels may only have a single (potential) reader. They can, of course, have multiple writers.

To make a choice between a set of channel reads, the channels have to be held in a Java array. If they are individual channels, this is still easy to arrange – for example:

```java
Channel[] c = {panic, supply, service};
```

We also need an instance of a class we have called Alternative in order to make our selection:

```java
Alternative alt = new Alternative();
```

where we refer to [1] for a description of its implementation. The term Alternative comes from the occam ALT constructor. We will sometimes refer to this choice mechanism as alting. We make our choice as follows:

```java
int i = alt.select(c);
int x = c[i].read();
... some process (which can make use of the value of i)
```

If there are one or more writers who have already written to one or more of the channels, the alt.select will return immediately with the index of one of them. In fact, the selection is prioritised so that, if there is a choice, it will choose the lowest index.

If there are no writers pending, the alt.select will block (passively – consuming no processor time) until one or more writers appear. It will then behave as above.

After receiving the chosen index, it is our responsibility to read from the channel selected – if we don’t, bad things will happen. After reading from the selected channel, we may engage in actions appropriate to the processing of the message and the channel from which it was received.

Often, the channel array will be small (and, if the channels are carrying Java ‘Objects’, each element can be communicating a separate protocol). In such cases, a ‘switch’ statement may be more convenient:

```java
switch (alt.select(c)) {
    case 0: {
        status = panic.read(); // panic == c[0]
        ... take evasive action
        break;
    }
```
case 1: {
    goods = supply.read (); // supply == c[1]
    ... update accounts
    break;
}

case 2: {
    order = service.read (); // service == c[2]
    ... process the order
    break;
}
}

We can impose run-time determined conditions that can be used to mask out some of the channels over which we are altering. We just set up an array of boolean guards with the same size as the channel array. Then:

```
{ int i = alt.select (c, guard);
  x = c[i].read ();
  ... some process (which can make use of the value of i)
}
```

What happens now is that if `guard[j]` is false, channel `c[j]` will be ignored when making this choice – even if it has a writer pending. Note that the guards are evaluated just once at the start of the selection – it would, of course, be a bad program that indulged in the race hazard of having another thread alter the values of these guards whilst this operation was being conducted!

Reference [1] gives a much fuller account of the material in this section, including the setting of timeouts on waiting for channels and for simple polling of the channels.

3.6 Wot, no chickens : WYSIWYG and safe

Let’s do the “Wot, no chickens?” example safely and simply, using channels to connect everything together. Figure 3 is a diagram of the network.

![Figure 3: The greedy and non-starving philosopher and his mates](image)

This time the canteen is an active object – a pure server process for its philosopher and chef clients. It listens on its supply and service channels, giving priority to the former.

The philosophers share a pair of channels – service and deliver. Philosophers eat chickens. They queue up at the canteen on the service channel to place their orders. The canteen refuses to accept any order when it has no chickens. This is a crucial difference from the previous version. The canteen is a live process and can make its own decisions
and impose its will. Previously, the canteen was passive and the philosophers had to barge in, discover the absence of food ("Wot, no chickens?") and do something to sort out the resulting mess.

When the canteen has some supplies, it will accept orders from service and dispense chickens down the deliver channel. It is always prepared to accept supplies from the supply channel.

The chef cooks chickens. When a batch is ready, she queues up at the canteen on its supply channel. Setting down the batch takes around 3 seconds and she is made to hang about until this has happened – this is to stay in line with the behaviour of the original system (that caused starvation). Here is the code for the chef:

```java
class Chef extends Thread {
    private Channel supply;
    
    public Chef (Channel supply) {
        this.supply = supply;
        start();
    }

    public void run () {
        try {
            ... starting ("Hello from the chef ...")
            while (true) {
                int n_chickens;
                ... sing ("Frying tonite ...")
                ... cook (takes around 2 seconds)
                n_chickens = 4;
                ... announce ("4 chickens, ready-to-go ...")
                supply.write (n_chickens); // supply the chickens
                supply.write (0); // wait till they’re set down
            }
        } catch (InterruptedException e) {}}
}
```

where we are obliged to put in an exception handler in case any of the channel methods fail. This process repeatedly executes a typical client transaction: it decides when it wants to start the transaction (the first supply.write) and commits itself to complete the transaction (the second supply.write).

The philosopher processes also behave as clients:

```java
class Phil extends Thread {
    private int id;
    
    private Channel service;
    private Channel deliver;
    
    public Phil (int id, Channel service, Channel deliver) {
        this.id = id;
        this.service = service;
        this.deliver = deliver;
        start();
    }
}
```
public void run () {
    try {
        ... starting ("Hello from philosopher " + id + " ...")
        while (true) {
            int chicken;
            if (id > 0) {
                ... think for around 3 seconds
            }
            ... announce ("Phil " + id + " ... gotta eat ...")
            service.write (0);   // may have to wait here
            chicken = deliver.read (); // never get blocked here
            ... consume ("Phil " + id + " ... mmm ... that’s good ...")
        }
    } catch (InterruptedException e) {} }
}

The canteen process is a pure server – it never initiates anything external, but responds (depending on its state) to client requests:

class Canteen extends Thread {
    private Channel service;   // shared (many-1)
    private Channel deliver;   // shared (but used 1-1)
    private Channel supply;    // not shared (1-1)
    public Canteen (Channel service, Channel deliver, Channel supply) {
        this.service = service;
        this.deliver = deliver;
        this.supply = supply;
        start ();
    }
    public void run () {
        try {
            Alternative alt = new Alternative ();   // alt object
            Channel[] c = {supply, service};   // alt channels
            boolean[] guard = {true, false}; // alt guards
            final int supply_index = 0;  // constant
            final int service_index = 1;  // constant
            int n_chickens = 0;  // variable
            ... starting ("Hello from canteen ...")
            while (true) {
                guard[service_index] = (n_chickens > 0);
                switch (alt.select (c, guard)) {
                    case supply_index: {
                        int value = supply.read ();  // new batch of chickens
                        ... ouch ("This dish is hot ...")
                        ... take 3 seconds to set down the dish
                        n_chickens += value;
                        ... announce (n_chickens + " now available ...")
                        value = supply.read ();  // let the chef go
                        break;
                    }
Each case of the switch corresponds (roughly) with the synchronised get and put methods of the passive monitor in Section 2.6. However, this time there are no dangerous loops and each case can be understood without reference to the other.

Finally, the network itself is constructed with the following code (which could go inside the main Java method):

```java
int n_philosophers = 5;
Channel service = new Channel();
Channel deliver = new Channel();
Channel supply = new Channel();
Canteen canteen = new Canteen(service, deliver, supply);
Chef chef = new Chef(supply);
Phil[] phil = new Phil[n_philosophers];
for (int i = 0; i < n_philosophers; i++) {
    phil[i] = new Phil(i, service, deliver);
}
```

This time, even though philosopher 0 is just as greedy, nobody starves. Philosopher 0 arrives at the service channel first, but is blocked there since the canteen has no chickens. The chef delivers between seconds 2 and 5, locking up the canteen as it services the delivery. At second 3, the other 4 philosophers also arrive at the service channel and queue up behind philosopher 0 – in the previous version, the greedy philosopher was stuck in the standby area inside the canteen. At second 5, philosophers 0 through 3 get served (because only 4 chickens were delivered) and philosopher 4 remains in line. The next time more chickens arrive, philosopher 4 will be at the head of the line.

The system is fair and deadlock/livelock/starvation-free. The system conforms to well-defined client-server design rules for which there are CSP theorems [16, 17, 18, 19, 20, 21] that prove these somewhat essential properties.
3.7 Buffers: WYSIWYG and safe

As our last example, we return to the Buffer from Section 2.5. Because of the restriction to alting only over channel reads, the consumer of this Buffer has to make a request before it can take anything. Notice the guards on selection that refuse consumer requests when the buffer is empty and refuse supplier inputs when the buffer is full.

class Buffer extends Thread {

    private Channel in; // could be shared (many-1)
    private Channel request; // could be shared (many-1)
    private Channel out; // could be shared (but used 1-1)

    private int[] buffer; // space to hold buffered data
    private int max; // size of buffer

    public Buffer (int max, Channel in, Channel request, Channel out) {
        this.max = max;
        this.in = in;
        this.request = request;
        this.out = out;
        buffer = new int[max];
        start ();
    }

    public void run () {
        try {
            int size = 0; // number of items currently held
            int lo = 0; // index of oldest item (when size > 0)
            int hi = 0; // index of next free slot (when size < max)

            Alternative alt = new Alternative (); // alt object
            Channel[] c = {in, request}; // alt channels
            boolean[] guard = {true, false}; // alt guards
            int in_index = 0; // constant
            int request_index = 1; // constant

            while (true) {
                guard[in_index] = (size < max); // only if there’s room
                guard[request_index] = (size > 0); // only if not empty
                switch (alt.select (c, guard)) {
                case 0: { // in_index
                    buffer[hi] = in.read (); // into first free slot
                    hi = (hi + 1) % max; // up the pointer
                    size++; // maintain the size
                    break;
                }
                case 1: { // request_index
                    int dummy = request.read (); // must take the request
                    out.write (buffer[lo]); // send oldest data
                    lo = (lo + 1) % max; // up the pointer
                    size--; // maintain the size
                    break;
                }
                }
            }
        } catch (InterruptedException e) {}
This Buffer is safe for use by any number of supplier and consumer threads – all are fairly queued on their respective access channels. All suppliers are blocked when the buffer is full. All consumers are blocked when the buffer is empty. When the blocks are removed, processes are serviced in the order they were queued – nobody is exposed to the danger of being (forever) overtaken.

We claim that this code is significantly easier to write and understand than the previous monitor version and that it is safe (whereas the monitor version is not). The responses of Buffer to each signal it receives from the outside world are short and independent of each other. The guarding of the alt channels, made possible by the liveness of this process, stops any mess happening due to signals being accepted at inappropriate times – since there is no mess to clean up, the code is very simple.

4 Summary

We have outlined the raw mechanisms for threads in Java and for synchronising them via the monitor methods provided. We have shown the difficulties of reasoning with monitors (whose semantics require a consideration of all their methods at the same time) – difficulties which are compounded by an incomplete rendering of the ideas presented in Hoare’s paper [13]. We have presented a channel model for synchronisation and communication that is directly based on Hoare’s (later) algebra of CSP [7, 8] and its practical realisation in occam [12].

We suggest that multi-threaded systems can and should be designed without user involvement in the coding of monitors (i.e. without using the key-word synchronized or the wait/notify methods or, even, the suspend/resume ones). The occam/CSP approach to Java (which, for the moment, we have christened JavaPP [2]) provides the foundation for the creation of reliable and safe applications. The semantics of the system – whether treated formally or intuitively – are compositional, which means that the meaning of an individual thread fragment does not depend on what other threads may be doing (What You See Is What You get). Analysis of systems for deadlock/livelock/starvation properties can exploit the large body of knowledge and tools that have been developed over the last decade for CSP. Even better, higher level CSP design rules (with tool support) may be applied that provide automatic guarantees against the presence of such dangerous attributes.

Of course, without changing the Java language, we cannot match the full security rigour (or even the performance) achieved by a CSP-aware language as occam, but these are significant wins. The JavaPP class libraries are, currently, implemented via the Java monitor methods (and described in this paper). We are looking to see if it is possible to substitute something based on the occam multi-processing kernels (which are specifically geared to support the CSP primitives) for the underlying threads libraries supporting the JVM. These kernels manage process context-switches and process startup/shutdowns in well under a microsecond – around 250 nanoseconds on a fast SPARC Ultra, compared with around 50 microseconds for the equivalent Java on the same processor. The benefit of these very low overheads is that we feel no constraints in designing with lots and lots of threads. The benefit of that is that we get closer to the real-world system we are trying to model and which, ultimately, pays the bills.

References


