

# An Algorithm to Translate PARADIGM specifications to PLTL in Polynomial Time

Rodolfo Sabas Gomez \*  
Computing Laboratory,  
Dept. of computer Science,  
University of Kent,  
CT2 7NZ Canterbury,  
Kent, United Kingdom  
+44 (0) 1227 823824  
rsg2@ukc.ac.uk

Juan Carlos Augusto  
Department of Electronics and  
Computer Science,  
University of Southampton,  
SO17 1BJ Southampton,  
Hampshire, United Kingdom  
+44 (0) 23 8059 3440  
jca@ecs.soton.ac.uk

Silvia Teresita Acuña  
Universidad Nacional de  
Santiago del Estero,  
Avenida Belgrano (S) 1912,  
(4200) Santiago del Estero,  
Santiago del Estero, Argentina  
+54 (0) 385 4509550  
silvac@unse.edu.ar

## ABSTRACT

PARADIGM has recently emerged as a new language to design cooperative object-oriented systems. To our knowledge, PARADIGM temporal aspects have not been studied before.

Here we describe a polynomial algorithm to translate PARADIGM models to Propositional Linear Temporal Logic programs. The resulting program is an executable specification of the modelled system, suitable for verifying model properties. It is also a declarative view of the model. Therefore we provide a temporal framework to understand and reason about PARADIGM models behavior, and system development in general. Finally, we believe this work provides further evidence on the benefits that PARADIGM has to offer to the Software Engineering community. We complement a previous conference paper which introduced the main concepts behind the translation process and its application in system verification.

## Keywords

Distributed systems, temporal logic, Specification Languages

## 1. INTRODUCTION

PARADIGM [14] is a high-level, visual, object-oriented modelling language to design cooperative systems. It is the sublanguage of SOCCA [8] used for modelling object communication, coordination and cooperation. PARADIGM appears as a promising approach to the design of complex systems (see e.g. [15], [7], and [1]).

Propositional Linear Temporal Logic (PLTL) has been used both in system specification and verification [13]. A number of tools have been proposed to accomplish such tasks, notably STeP [4] and SPIN [11]. In the STeP framework the specification language SPL (that means Simple Programming Language) can be used to specify a system that is translated to a Fair Transition System. Then, behavior properties expressed by temporal logic formulas can be verified using a deductive approach. In the SPIN framework a system is specified using the Promela language to represent a system conceived through a Global State Automata. Then temporal logic formulas can again be verified but in this case using the model checking technique. Other approaches to verification are based on more complex temporal assumptions like branching time, e.g. Kronos [16], here we focus on linear time leaving verification over branching time and other issues for future exploration.

We show that is possible to translate a PARADIGM model into a PLTL program, thus obtaining an executable specification. The resulting PLTL program will be composed by a number of logic rules implying, at any time, the current state of process executions. Furthermore, these rules can be entirely generated from the information provided in any PARADIGM model. This paper focuses on the translation algorithm (a Prolog implementation is discussed in [2]). This work complements the results presented in [3], which was mainly concerned with translation concepts and its application in verification.

One benefit that can be expected from such a translation is that the temporal logic framework allows us to prove correctness properties about the system behavior by automatic means. Properties are intended to be expressed as queries to a PLTL interpreter (see e.g. [6]) with the logic program as a knowledge base. The interpreter can be also expected to be used as a simulation tool: process executions can be traced to any situation of interest. This feature can be useful during design stages: we can change the PARADIGM model, translate it to a logic program, and study the process behavior until requirements have been met. Finally, the logic approach offers a different, declarative way for studying PARADIGM models. It provides a possible temporal framework for system development. We therefore aim to enhance the current knowledge on PARADIGM and its benefits in system development.

**Paper organization:** Section 2 and 3 offer the necessary overview on PARADIGM and PLTL, respectively. Section 4 presents the concepts behind the translation algorithm, which is properly introduced in section 5. Section 7 shows some examples of verification properties, and conclusions are given in section 8.

## 2. PARADIGM

PARADIGM models a dynamic system as a set of parallel processes. Processes are modelled as state transition diagrams (STD's from now on), and they can be assigned a role of employees or managers. Managers coordinate their employees by prescribing them a proper set of subprocesses.

A subprocess is a temporal constraint placed on the employee behavior. It is modelled as an STD which inherits a subset of employee states and transitions, meaning that as long as this subprocess is prescribed the employee can only achieve part of its complete behavior. Because an employee can be controlled by several managers, its behavior at anytime results from the composite behavior assigned by each of its currently prescribed sub-

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processes. In other words, employee transitions can only be performed if they are allowed in all subprocesses that are currently prescribed to the employee in question. For simplicity, we assume all processes in the PARADIGM model are always active.

Traps model those execution stages where employees need coordination. They are defined as being a subset of subprocess states. Once an employee enters the first state of those defining a trap, the manager which prescribed the subprocess containing that trap is notified, and the employee can only perform transitions within the trap.

Manager states are assigned to a set of subprocesses, one per employee. This set is currently prescribed as long as the manager remains in that state, but it is possible for a subprocess to be prescribed in several manager states. A manager cannot prescribe, at a given time, more than one subprocess per employee.

Manager transitions are assigned to a set of traps which must be entered for the transition in question to be performed. Employee executions cannot proceed outside of traps until the manager prescribes the right set of subprocesses, thus changing their behavior restrictions, and in the other way managers cannot proceed until the right employees are inside their traps. An interesting example of a PARADIGM model is explained in [8].

### 3. THE TEMPORAL LOGIC

The system is thought as evolving along a (possibly finite) sequence of states  $\sigma = s_0, s_1, \dots$  where  $s_0$  is the initial state. Notice that no final state is enforced in that sequence of states. This allows the consideration of reactive systems which is a class of systems that PARADIGM is well equipped to deal with. Each state  $s_i$  is defined as a set of atomic propositions holding at that execution stage. After  $n$  steps a computation  $\sigma = s_0, \dots, s_n$  had gone through  $|\sigma| = n + 1$  states. Time here is used to refer to the stage sequence the system goes through, so it is linear and with future unbounded. We assume a propositional language  $\mathcal{L}_{\mathcal{P}}$  based on the traditional temporal operators  $\Diamond A$  ( $A$  is true in some future state) and  $\Box A$  ( $A$  is always true from the next state on). Here we only consider the future fragment, which is enough to highlight verification possibilities. Other well known operators like  $\bigcirc$  (next),  $\mathcal{U}$  (until) and the past fragment can be added to the proposal in the future with interesting benefits during the verification stage. The set of well formed formulas of the temporal language can be defined inductively as follows ( $p$  is an atomic proposition):

$$\phi = p \mid \neg\phi \mid \phi_1 \wedge \phi_2 \mid \phi_1 \vee \phi_2 \mid \phi_1 \rightarrow \phi_2 \mid \Diamond\phi \mid \Box\phi$$

Formula semantics is shown below w.r.t. a pair  $(\sigma, t)$  where  $\sigma = s_0, s_1, \dots, s_t, \dots$ :

$(\sigma, t) \models p$	iff $p \in s_t$ with $p$ atomic
$(\sigma, t) \models \neg\phi_1$	iff $(\sigma, t) \not\models \phi_1$
$(\sigma, t) \models \phi_1 \vee \phi_2$	iff $(\sigma, t) \models \phi_1$ or $(\sigma, t) \models \phi_2$
$(\sigma, t) \models \phi_1 \wedge \phi_2$	iff $(\sigma, t) \models \phi_1$ and $(\sigma, t) \models \phi_2$
$(\sigma, t) \models \phi_1 \rightarrow \phi_2$	iff $(\sigma, t) \not\models \phi_1$ or $(\sigma, t) \models \phi_2$
$(\sigma, t) \models \Diamond\phi$	iff exists $s > t : (\sigma, s) \models \phi$
$(\sigma, t) \models \Box\phi$	iff for all $s > t : (\sigma, s) \models \phi$

This language provides a set of well formed formulas which is expressive enough to encode a PARADIGM model in a declarative way. It also provides the means to express well known schema formulas [12] used in system verification, like  $\Box\phi$  (*safety*) and others from the “liveness family” like  $\Diamond\phi$  (*guarantee*),  $\Box(\phi_1 \rightarrow \Diamond\phi_2)$  (*response/recurrence*),  $\Diamond\Box\phi$  (*persistence*) and  $\Box\Diamond\phi_1 \rightarrow \Box\Diamond\phi_2$  (*progress*). The framework requires sets of

propositions whose cardinality depends on the sets of manager and employee processes. Modularity principles applied over the PARADIGM model should keep these sets reasonably small. Finally, we give our temporal logic a *persistence semantics*: propositions preserve their truth values until it is explicitly changed by a rule, and, unless otherwise implied, propositions are assumed to be false by default. This will be consistent with our logic programming implementation of a PLTL interpreter.

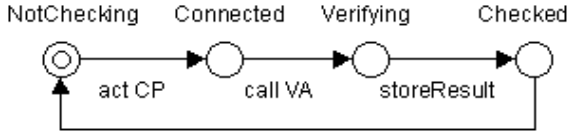
### 4. THE TRANSLATION

The goal of the translation process is to produce a PLTL program,  $\mathcal{P}$ , which simulates the behavior of the processes included in the PARADIGM model. Process executions are mapped to the state-sequence semantics of the temporal logic. We call these states global states in contrast to state changes in STDs appearing in the PARADIGM model. Every global state will be a set of propositions of three possible different kinds: a) proposition  $st$ , where  $st$  denotes a state of a given process  $p$ , will be true anytime  $p$  remains on  $st$ , b) proposition  $sp$ , where  $sp$  denotes a subprocess of a given employee  $e$ , will be true anytime  $sp$  remains prescribed to  $e$  and c) proposition  $tp$ , where  $tp$  denotes a trap of a given employee  $e$ , will be true anytime  $e$  remains inside  $tp$ . State changes in PARADIGM processes can be seen as a transformation of the global state at time  $t$ ,  $G_t$ , into a global state at time  $t + n$ ,  $n \in \mathbb{N}$ ,  $G_{t+n}$ . Where  $n \in \mathbb{N}$  represents the duration of the execution of the transition being considered.

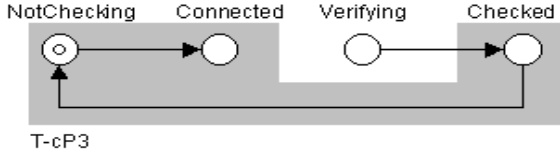
We will assume that all propositions denoting states, subprocesses and traps are unique. For example, propositions  $cpNotChecking$ ,  $cpS3$  and  $tcp3$  denote, respectively, that process `checkPIN` is currently in state `NotChecking`, that subprocess `checkPIN_s3` is currently prescribed and that `checkPIN` is currently inside trap `T-cp3`. Rules in  $\mathcal{P}$  will simulate PARADIGM dynamics, asserting or denying the truth of propositions depending on execution stages. These rules will be conceptually introduced in sections 4.1, 4.2, 4.3, 4.4 and 4.5.

Process transitions modify the global state in different ways, and in turn global states impose different restrictions on employee and manager transitions. Therefore transitions will be modelled by rules of the form:  $\Box(Pre \rightarrow \Diamond Pos)$ , where  $Pre$  is a set of preconditions which must hold on  $G_t$  to perform the state change, and  $Pos$  is a set of postconditions holding on the new global state  $G_{t+n}$ , after the change. So rules will only express the order in which states can be visited. This is due to PARADIGM’s lack of information concerning the time that processes spend inside states and the time that transitions require to be performed.

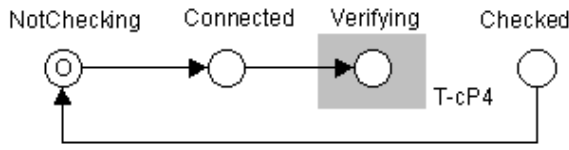
Rules composing  $\mathcal{P}$  will be illustrated through a simpler version of the example given in [8]. Figs. 1 to 6 show part of a PARADIGM model for an Automatic Teller Machine (see [2] for a more detailed example). Process `checkPIN` (Fig. 1) is responsible for checking user’s PIN on his magnetic card, but to do this it needs to call process `verifyAccount` (Fig. 4). Both processes are employees of manager `BankComputer` (Fig. 6 shows a subset of the proper STD), which coordinates the caller-called relationship by prescribing each employee a different set of subprocesses as needed. Figs. 2 and 5 show the subprocesses that can be prescribed by `BankComputer` to `checkPIN` and `verifyAccount`, respectively. `checkPIN` is also employee of manager `ATM`, but it is not included in our example. However it is important to show (Fig. 3) which subprocesses can be prescribed to `checkPIN` by `ATM`. Traps are shown as shaded boxes.



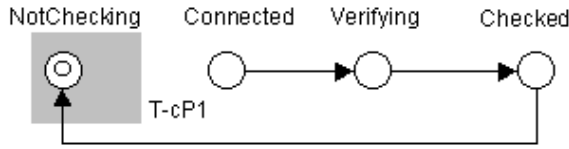
**Figure 1: Employee process checkPIN**  
checkPIN\_s3



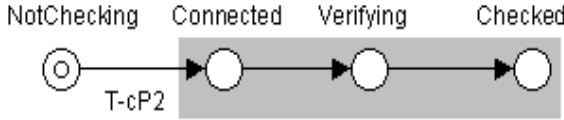
checkPIN\_s4



**Figure 2: Sprocs. of checkPIN (BankComputer)**  
checkPIN\_s1



checkPIN\_s2

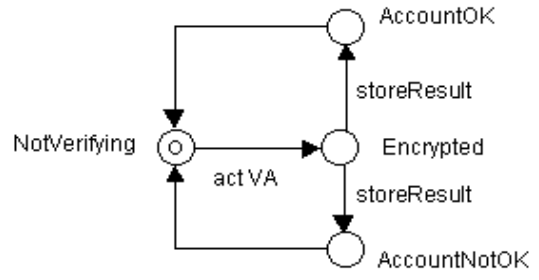


**Figure 3: Sprocs. of checkPIN (ATM)**

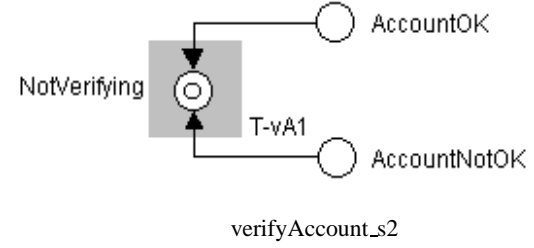
#### 4.1. Employee transitions

These kind of rule models a given transition  $ts_{ij}$  from state  $st_i$  to  $st_j$  in employee  $e$ . This transition is allowed only if  $e$  is currently on  $st_i$  and  $ts_{ij}$  is allowed in all subprocesses that are currently prescribed to  $e$ . This set of subprocesses cannot be known in advance, but fortunately there is another way to express the same requirement. Let  $M_e = \{m_1, \dots, m_q\}$  be the set of all managers for  $e$  and  $S_r = \{sp_1^r, \dots, sp_n^r\}$  the set of all subprocesses which can be prescribed to  $e$  by any  $m_r \in M_e$ , such that  $ts_{ij}$  is allowed in  $sp_k^r$ , for all  $1 \leq k \leq n$ . Then  $ts_{ij}$  can be performed if, for each manager  $m_r$ , at least one of the subprocesses in  $S_r$  is currently prescribed. Let sets  $S_1, \dots, S_q$  denote the subprocesses prescribed by managers  $m_1, \dots, m_q$  (and constrained as mentioned before); and suppose they are, respectively:  $\{sp_1^1, \dots, sp_r^1\}, \dots, \{sp_1^q, \dots, sp_s^q\}$ . Finally the rule expresses that after the change  $e$  will be no longer in state  $st_i$  but in  $st_j$ :

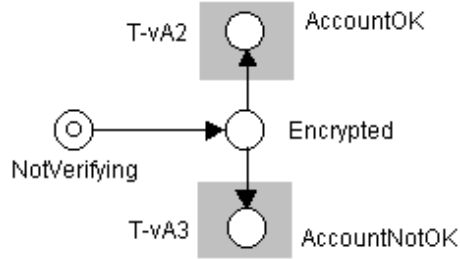
$$\square((st_i \wedge (sp_1^1 \vee \dots \vee sp_r^1) \wedge \dots \wedge (sp_1^q \vee \dots \vee sp_s^q)) \rightarrow \Diamond(\neg st_i \wedge st_j))$$



**Figure 4: Employee process verifyAccount**  
verifyAccount\_s1



verifyAccount\_s2



**Figure 5: Subprocesses of verifyAccount**

**EXAMPLE 1** Consider transition “call VA” from Connected to Verifying in checkPIN (Figs. 3 and 2). It is allowed in checkPIN\_s1 and checkPIN\_s2 (prescribed by ATM), and checkPIN\_s4 (prescribed by BankComputer). Therefore either checkPIN\_s1 or checkPIN\_s2, and checkPIN\_s4 must be prescribed for the transition to be performed (“(cPs1∨cPs2)∧cPs4”):

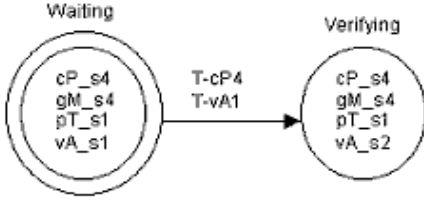
$$\square((cpConnected \wedge ((cPs1 \vee cPs2) \wedge cPs4)) \rightarrow \Diamond(\neg cpConnected \wedge cpVerifying)) \quad \Delta$$

Note that it is also possible that other outgoing transitions from state  $st_i$  are included in the same subprocesses  $S_1, \dots, S_q$ . Let  $st_j^2, st_j^3, \dots, st_j^u$  be the after states in question, and  $\oplus$  the exclusive ‘or’ operator ( $A \oplus B \equiv ((A \wedge \neg B) \vee (\neg A \wedge B))$ ). Then the general rule schema becomes:

$$\square((st_i \wedge (sp_1^1 \vee \dots \vee sp_r^1) \wedge \dots \wedge (sp_1^q \vee \dots \vee sp_s^q)) \rightarrow \Diamond(\neg st_i \wedge (st_j \oplus st_j^2 \oplus st_j^3 \oplus \dots \oplus st_j^u)))$$

#### 4.2. Manager transitions

These kind of rule models a given transition  $ts_{ij}$  from state  $st_i$  to  $st_j$  in manager  $m$ . This transition is allowed only if  $m$  is currently on  $st_i$  and the right employees are currently inside the traps related with  $ts_{ij}$ . This set of subprocesses cannot be known in advance, but fortunately there is another way to express the same requirement. The rule also expresses that after the transition has been performed  $m$  is no longer in  $st_i$  but in  $st_j$ , and therefore that the set of currently prescribed subprocesses



**Figure 6: Manager process BankComputer (fragment)**

has been (possibly) changed. In fact, it is possible that some of those subprocesses prescribed on  $st_i$  are no longer prescribed on  $st_j$ , or remain prescribed on  $st_j$  or even that new subprocesses are prescribed on  $st_j$ .

Let  $\{tp_1, \dots, tp_n\}$  be the set of traps related with  $ts_{ij}$ ,  $\{sp_1, \dots, sp_m\}$  the set of subprocesses prescribed on  $st_i$  but not on  $st_j$ , and  $\{tp_q, \dots, tp_u\}$  the set of traps included in any  $sp_i$ ,  $1 \leq i \leq m$ . We will see that all new subprocesses that are prescribed in  $st_j$  but not in  $st_i$  are handled by other kind of rule (section 4.3). Finally, those propositions denoting subprocesses that remain prescribed from  $st_i$  to  $st_j$  do not require any action, i.e., they are not explicitly asserted nor denied and thus remain true (persistence semantics). The rule is shown below:

$$\begin{aligned} & \Box((st_i \wedge (tp_1 \wedge \dots \wedge tp_n)) \\ & \rightarrow \Diamond(\neg st_i \wedge st_j \wedge (\neg sp_1 \wedge \dots \wedge \neg sp_m) \\ & \wedge (\neg tp_q \wedge \dots \wedge \neg tp_u))) \end{aligned}$$

**EXAMPLE 2** Consider the transition from *Waiting* to *Verifying* in *BankComputer* (Fig. 6). This change cannot be performed until both traps *T-cP4* and *T-vA1* have been entered ("*tcP4*  $\wedge$  *tvA1*"). Once the manager is in state *Verifying*, subprocess *verifyAccount\_s1* is no longer prescribed and thus trap *T-vA1* is left (" $\neg$  *vAs1*  $\wedge$   $\neg$  *tvA1*"):

$$\begin{aligned} & \Box((bcWaiting \wedge tcP4 \wedge tvA1) \\ & \rightarrow \Diamond(\neg bcWaiting \wedge bcVerifying \wedge \\ & \neg vAs1 \wedge \neg tvA1)) \end{aligned} \quad \Delta$$

Previous rules model the time each employee and manager process remain in their states. However, this time depends on the dynamics of subprocesses and traps. Following rules assert that knowledge.

#### 4.3. Subprocess prescription

This kind of rule models the time subprocesses remain prescribed to their employees. Specifically, for every state of a manager process there will be a rule expressing the set of subprocesses that are prescribed while the manager remains in that state. Let  $st_i$  be a manager state and  $\{sp_1, \dots, sp_n\}$  the subprocesses which are prescribed in this state. The rule is shown below:

$$\Box(st_i \rightarrow (sp_1 \wedge \dots \wedge sp_n))$$

**EXAMPLE 3** Consider the subprocesses that *BankComputer* prescribes while it is in state *Waiting* (Fig. 6), like *checkPIN\_s4* ("*cPs4*") and *verifyAccount\_s1* ("*vAs1*"):

$$\begin{aligned} & \Box(bcWaiting \\ & \rightarrow (cPs4 \wedge gMs4 \wedge pTs1 \wedge vAs1)) \end{aligned} \quad \Delta$$

#### 4.4. Traps

This kind of rule models the time employees remain inside their traps. Specifically, for every trap  $tp$  in subprocess  $sp$ , where  $sp$  is a subprocess of employee  $e$ , there will be a rule expressing that  $e$  is currently inside  $tp$  if  $e$  is in any state  $st_1, \dots, st_n$  included in  $tp$ . Rule is shown below:

$$\Box((sp \wedge (st_1 \vee \dots \vee st_n)) \rightarrow tp)$$

**EXAMPLE 4** Employee *checkPIN* remains inside trap *T-cP2* as long as it is prescribed subprocess *checkPIN\_s2* and remains in states *Connected*, *Verifying* or *Checked*:

$$\begin{aligned} & \Box((cPs2 \wedge \\ & (cpConnected \vee cpVerifying \vee cpChecked)) \\ & \rightarrow tcP2) \end{aligned} \quad \Delta$$

#### 4.5. Initial conditions

We provide a rule to set propositions at the first global state. Here we coordinate processes as starting execution in their initial states, but different rules may be provided to change the initial execution conditions.

Let  $\{st_1, \dots, st_n\}$  be the set of processes initial states (subprocesses initially prescribed are inferred according to the rules of section 4.3). The translation will generate the fact *init*, a proposition which will only hold at the initial time, and the following rule:

$$init \rightarrow (st_1 \wedge \dots \wedge st_n)$$

**EXAMPLE 5** The rule below specify the initial states of employees *checkPIN*, *verifyAccount* and manager *BankComputer*:

$$\begin{aligned} & init \rightarrow \\ & (cpNotChecking \wedge vaNotVerifying \wedge bcWaiting) \end{aligned} \quad \Delta$$

Note that the assertion of *bcWaiting* as initial state implies a set of initial subprocesses *cPs4*, *gMs4*, *pTs1*, *vAs1* by virtue of the rule shown in example 3, and in turn, because of *vAs1* and *vaNotVerifying*, this also implies that *tvA1* holds (fig. 5). Also, and according to our persistence semantics, all other propositions, i.e. the rest of states, subprocesses and traps which are not mentioned nor implied, are assumed to be false in the initial state.

### 5. THE ALGORITHM

In this section the translation process will be described as a set of steps that takes a *PARADIGM* model as input and generates a *PLTL* program as output. The *PARADIGM* model is assumed to be correct, and contains all the information needed by the algorithm: processes, subprocesses, states, traps and some of their relationships. This information is modelled as a collection of sets (section 5.1), which is a suitable form where future implementations can be obtained from. The algorithm itself will be described in natural language (section 5.2).

## 5.1. Algorithm inputs

The sets that are shown below encode those elements of the PARADIGM model which are needed by the translation process. We do not assume any particular tool for constructing these sets. For the sake of space economy, we have chosen a set of labels for denoting processes, states, subprocesses and traps which are shorter than those appearing in the figures. However, these labels are quite obvious and easy to recognize. For example, *cPs4* denotes subprocess *checkPIN\_s4*. Input sets comprise the following (examples refer to the Automatic Teller Machine case study described in section 4):

1. The set *EMP* of employee processes. For example,

$$EMP = \{\text{checkPIN}, \text{verifyAccount}, \dots\}$$

2. The set *MAN* of manager processes. For example,

$$MAN = \{\text{atm}, \text{bankComputer}, \dots\}$$

3. The set *PRO<sub>trs</sub>* of transitions in every process.  $PRO_{trs} = \bigcup_{i=1}^n \{(p_i, \bigcup_{j=1}^m \{(st_j, st_k)\})\}$ ,  $1 \leq k \leq m$ , where  $p_i$  denotes a process and  $(st_j, st_k)$  denotes a transition from state  $st_j$  to state  $st_k$  in  $p_i$ :

$$\begin{aligned} PRO_{trs} = & \{(\text{checkPIN}, \\ & \{(\text{cpNotChecking}, \text{cpConnected}), \\ & (\text{cpConnected}, \text{cpVerifying}), \\ & (\text{cpVerifying}, \text{cpChecked}), \\ & (\text{cpChecked}, \text{cpNotChecking})\}), \\ & (\text{verifyAccount}, \\ & \{(\text{vaNotVerifying}, \text{vaEncrypted}), \\ & (\text{vaEncrypted}, \text{vaAccountOK}), \\ & (\text{vaEncrypted}, \text{vaAccountNotOK}), \\ & (\text{vaAccountOK}, \text{vaNotVerifying})\}), \\ & (\text{vaAccountNotOK}, \text{vaNotVerifying})\}) \\ & \dots\} \end{aligned}$$

4. The set *MAN<sub>spr</sub>* of subprocesses prescribed in every manager state.  $MAN_{spr} = \bigcup_{i=1}^n \{(st_i, \bigcup_{j=1}^m \{sp_j\})\}$  where  $st_i$  denotes a manager state and  $sp_j$  denotes a subprocess prescribed in  $st_i$ . For example,

$$\begin{aligned} MAN_{spr} = & \{(\text{bcWaiting}, \{\text{cPs4}, \text{gMs4}, \text{pTs1}, \text{vAs1}\}), \\ & (\text{bcVerifying}, \{\text{cPs4}, \text{gMs4}, \text{pTs1}, \text{vAs2}\}) \\ & \dots\} \end{aligned}$$

5. The set *TRP<sub>sta</sub>* of states defining every trap.  $TRP_{sta} = \bigcup_{i=1}^n \{(tp_i, \bigcup_{j=1}^m \{st_j\})\}$  where  $tp_i$  denotes a trap and  $st_j$  denotes a state inside trap  $tp_i$ . For example,

$$\begin{aligned} TRP_{sta} = & \{(\text{tcP1}, \{\text{cpNotChecking}\}), \\ & (\text{tcP2}, \\ & \{\text{cpConnected}, \text{cpVerifying}, \text{cpChecked}\}), \\ & (\text{tcP3}, \\ & \{\text{cpNotChecking}, \text{cpConnected}, \text{cpChecked}\}), \\ & (\text{tcP4}, \{\text{cpVerifying}\}), \\ & (\text{tvA1}, \{\text{vaNotVerifying}\}), \\ & (\text{tvA2}, \{\text{vaAccountOK}\}), \\ & (\text{tvA3}, \{\text{vaAccountNotOK}\}), \\ & \dots\} \end{aligned}$$

6. The set *SPR<sub>trp</sub>* of traps in every subprocess.

$$\begin{aligned} SPR_{trp} = & \bigcup_{i=1}^n \{(sp_i, \bigcup_{j=1}^m \{tp_j\})\} \text{ where } sp_i \text{ denotes} \\ & \text{a subprocess and } tp_j \text{ denotes a trap of } sp_i. \text{ For example} \\ SPR_{trp} = & \{(\text{cPs1}, \{\text{tcP1}\}), \\ & (\text{cPs2}, \{\text{tcP2}\}), \\ & (\text{cPs3}, \{\text{tcP3}\}), \\ & (\text{cPs4}, \{\text{tcP4}\}), \\ & (\text{vAs1}, \{\text{tvA1}\}), \\ & (\text{vAs2}, \{\text{tvA2}, \text{tvA3}\}) \dots\} \end{aligned}$$

7. The set *EMP<sub>spr</sub>* of subprocesses which can be prescribed by every manager to every employee.  $EMP_{spr} = \bigcup_{i=1}^n \bigcup_{j=1}^m \{(e_i, m_j, \bigcup_{k=1}^q \{sp_k\})\}$  where  $e_i$  denotes an employee,  $m_j$  denotes a manager for  $e_i$  and  $sp_k$  denotes a subprocess of  $e$  that can be prescribed by  $m_j$ . For example

$$\begin{aligned} EMP_{spr} = & \{(\text{checkPIN}, \text{atm}, \{\text{cPs1}, \text{cPs2}\}), \\ & (\text{checkPIN}, \text{bankComputer}, \{\text{cPs3}, \text{cPs4}\}), \\ & (\text{verifyAccount}, \text{bankComputer}, \{\text{vAs1}, \text{vAs2}\}) \\ & \dots\} \end{aligned}$$

8. The set *INI<sub>sta</sub>* of initial states.  $INI_{sta} = \bigcup_{i=1}^n \{ST_i\}$  where  $st_i$  denotes a process initial state.

$$\begin{aligned} INI_{sta} = & \{\text{cpNotChecking}, \text{vaNotVerifying}, \text{bcWaiting}, \\ & \dots\} \end{aligned}$$

9. The set *TRS<sub>spr</sub>* of subprocesses every employee transition is included in.

$$\begin{aligned} TRS_{spr} = & \bigcup_{i=1}^n \{((st_i, st_j), \bigcup_{k=1}^m \{sp_k\})\} \text{ for some} \\ & 1 \leq j \leq n, \text{ where } (st_i, st_j) \text{ denotes a transition of a given} \\ & \text{employee } E \text{ from state } st_i \text{ to state } st_j \text{ and } sp_k \text{ denotes a} \\ & \text{subprocess of } e \text{ containing such a transition. For example,} \end{aligned}$$

$$\begin{aligned} TRS_{spr} = & \{((\text{cpNotChecking}, \text{cpConnected}), \\ & \{\text{cPs2}, \text{cPs3}, \text{cPs4}\}), \\ & ((\text{cpConnected}, \text{cpVerifying}), \\ & \{\text{cPs1}, \text{cPs2}, \text{cPs4}\}), \\ & ((\text{cpVerifying}, \text{cpChecked}), \\ & \{\text{cPs1}, \text{cPs2}, \text{cPs3}\}), \\ & ((\text{cpChecked}, \text{cpNotChecking}), \\ & \{\text{cPs1}, \text{cPs3}, \text{cPs4}\}), \\ & ((\text{vaNotVerifying}, \text{vaEncrypted}), \{\text{vAs2}\}), \\ & ((\text{vaEncrypted}, \text{vaAccountOK}), \{\text{vAs2}\}), \\ & ((\text{vaEncrypted}, \text{vaAccountNotOK}), \{\text{vAs2}\}), \\ & ((\text{vaAccountOK}, \text{vaNotVerifying}), \{\text{vAs1}\}), \\ & ((\text{vaAccountNotOK}, \text{vaNotVerifying}), \{\text{vAs1}\}), \\ & \dots\} \end{aligned}$$

10. The set *MAN<sub>trp</sub>* of traps related with manager transitions.  $MAN_{trp} = \bigcup_{i=1}^n \{((st_i, st_j), \bigcup_{k=1}^m \{tp_k\})\}$  for some  $1 \leq j \leq n$ , where  $(st_i, st_j)$  denotes a transition of a given manager  $m$  from state  $st_i$  to state  $st_j$  and  $tp_k$  denotes a trap related with that transition. For example,

$$\begin{aligned} MAN_{trp} = & \{((\text{bcWaiting}, \text{bcVerifying}), \{\text{tcP4}, \text{tvA1}\}), \\ & \dots\} \end{aligned}$$

## 5.2. Algorithm steps

Now we describe the translation algorithm as a set of steps, each one taking one or more input sets (section 5.1) and generating a kind of rule for the PLTL program. We assume the existence of a procedure `generateRule()` which performs the output of a rule to the PLTL program. All variables are considered local to each step environment. Set variables are denoted with uppercase calligraphic letters, e.g.  $\mathcal{A}$ . Element variables are denoted with uppercase italic letters, e.g.  $A$ . Constant elements will be denoted with lowercase italic letters, e.g.  $a$ .

### 1) State changes in employee processes

INPUT:  $EMP$ ,  $PRO_{transitions}$ ,  $TRS_{subprocesses}$ ,  $EMP_{subprocesses}$

PROCEDURE:

```

% for each employee
Tmp1 := EMP
[1] Repeat until Tmp1 =  $\emptyset$ 
begin
  Let  $e \in Tmp1$ 
  Tmp1 := Tmp1 / { $e$ }
[2] Let  $T_e$  such that  $(e, T_e) \in PRO_{transitions}$ 
  % for each transition of this employee
  Tmp2 :=  $T_e$ 
  Generated :=  $\emptyset$ 
[3] Repeat until Tmp2 =  $\emptyset$ 
begin
  Let  $(st_i, st_j) \in Tmp2$ 
  Tmp2 := Tmp2 / {( $st_i, st_j$ )}
  %  $\mathcal{S}_{ij}$  is the set of all subprocesses
  % containing this transition
[4] Let  $\mathcal{S}_{ij}$  such that:
  (( $st_i, st_j$ ),  $\mathcal{S}_{ij}$ )  $\in TRS_{subprocesses}$ 
  %  $\mathcal{S}_e$  is the set of all subprocesses
  % prescribed by each manager to this
  % employee
[5] Let  $\mathcal{S}_e = \{\mathcal{S}_m \mid \exists m \in MAN$ 
  (( $e, m, \mathcal{S}_m$ )  $\in EMP_{subprocesses}$ )}
  % intersect each subset of  $\mathcal{S}_e$  with
  %  $\mathcal{S}_{ij}$ , and form the set  $\mathcal{S}_{ij}^m$ .
  %  $\mathcal{I} \subset \mathcal{S}_m$  expresses the optimization
  % described in sec. 4.1
[6] Let  $\mathcal{S}_{ij}^m = \{\mathcal{I} \mid \exists \mathcal{S}_m \in \mathcal{S}_e$ 
  ( $\mathcal{I} = \mathcal{S}_m \cap \mathcal{S}_{ij} \wedge \mathcal{I} \subset \mathcal{S}_m$ )}
[7] Let  $\mathcal{J} = \{st'_j \mid ((st_i, st'_j), \mathcal{S}_{ij}^m) \in TRS_{subprocesses}$ 
   $\wedge \forall \mathcal{I} \in \mathcal{S}_{ij}^m (\mathcal{I} \cap \mathcal{S}_{ij}^m \neq \emptyset)\}$ 
  if  $(st_i, \mathcal{J}, \mathcal{S}_{ij}^m) \notin Generated$ 
  then
    Suppose:
     $\mathcal{S}_{ij}^m = \{\{sp_1^1, \dots, sp_r^1\}, \dots, \{sp_1^q, \dots, sp_s^q\}\}$ 
     $\mathcal{J} = \{st_j^1, st_j^2, st_j^3, \dots, st_j^u\}$ 
[8] GenerateRule(
   $\square((st_i \wedge (sp_1^1 \vee \dots \vee sp_r^1) \wedge \dots \wedge (sp_1^q \vee \dots \vee sp_s^q))$ 
   $\rightarrow \Diamond(\neg st_i \wedge (st_j^1 \oplus st_j^2 \oplus \dots \oplus st_j^u)))$ 
  )
  Generated := Generated  $\cup \{(st_i, \mathcal{J}, \mathcal{S}_{ij}^m)\}$ 
end % {Repeat until Tmp2 =  $\emptyset$ }
end % {Repeat until Tmp1 =  $\emptyset$ }
```

### 2) State changes in manager processes.

INPUT:  $MAN$ ,  $PRO_{transitions}$ ,  $MAN_{traps}$ ,  $MAN_{subprocesses}$

PROCEDURE:

```

% for each manager
Tmp1 := MAN
[1] Repeat until Tmp1 =  $\emptyset$ 
begin
  Let  $m \in Tmp1$ 
  Tmp1 := Tmp1 / { $m$ }

  %  $T_m$  is the set of transitions of this
  % manager
[2] Let  $T_m$  be such that:
  ( $m, T_m$ )  $\in PRO_{transitions}$ 
  Tmp2 :=  $T_m$ 

  % for each transition of  $T_m$ 
[3] Repeat until Tmp2 =  $\emptyset$ 
begin
  Let  $(st_i, st_j) \in Tmp2$ 
  Tmp2 := Tmp2 / {( $st_i, st_j$ )}

  %  $T_{ij}$  is the set traps of this
  % transition, i.e. those traps that
  % must be entered for this transition
  % could be performed
[4] Let  $T_{ij}$  be such that:
  (( $st_i, st_j$ ),  $T_{ij}$ )  $\in MAN_{traps}$ 

  %  $\mathcal{I}$  is the set of subprocesses
  % prescribed in state  $st_i$ 
[5] Let  $\mathcal{I}$  be such that:
  ( $st_i, \mathcal{I}$ )  $\in MAN_{subprocesses}$ 

  %  $\mathcal{J}$  is the set of subprocesses
  % prescribed in state  $st_j$ 
[6] Let  $\mathcal{J}$  be such that:
  ( $st_j, \mathcal{J}$ )  $\in MAN_{subprocesses}$ 
   $\mathcal{D} = \mathcal{I} / \mathcal{J}$ 

  %  $T_{left}$  is the set of traps included
  % in subprocesses of  $\mathcal{D}$ , i.e. those
  % traps that are left after the
  % state change
[8] Let  $T_{left} = \{tp \mid \exists sp \in \mathcal{D}$ 
  (( $sp, T_{sp}$ )  $\in SPR_{traps} \wedge tp \in T_{sp}\})$ 
  Suppose  $T_{ij} = \{tp_1, \dots, tp_n\}$ 
  Suppose  $\mathcal{D} = \{sp_1, \dots, sp_m\}$ 
  Suppose  $T_{left} = \{tp_q, \dots, tp_u\}$ 
[9] GenerateRule(
   $\square((st_i \wedge (tp_1 \wedge \dots \wedge tp_n) \rightarrow$ 
   $\Diamond(\neg st_i \wedge st_j \wedge (\neg sp_1 \wedge \dots \wedge \neg sp_m)$ 
   $\wedge (\neg tp_q \wedge \dots \wedge \neg tp_u)))$ 
  )
  end % {Repeat until Tmp2 =  $\emptyset$ }
end % {Repeat until Tmp1 =  $\emptyset$ }
```

### 3) Subprocess prescriptions

INPUT:  $MAN_{subprocesses}$

PROCEDURE:

```
% for each manager state
  Tmp1 :=  $MAN_{subprocesses}$ 
[1] Repeat until Tmp1 =  $\emptyset$ 
  begin
    %  $\mathcal{S}_{st}$  is the set of all subprocesses
    % prescribed in this state
    Let  $(st, \mathcal{S}_{st}) \in Tmp1$ 
    Tmp1 := Tmp1 /  $\{(st, \mathcal{S}_{st})\}$ 
    Suppose  $\mathcal{S}_{st} = \{sp_1, \dots, sp_n\}$ 
[2] GenerateRule(  $\Box(st \rightarrow (sp_1 \wedge \dots \wedge sp_n))$  )
  end % {Repeat until Tmp1 =  $\emptyset$ }
```

### 4) Inside a trap.

INPUT:  $SPR_{traps}$ ,  $TRP_{states}$

PROCEDURE:

```
% for each subprocess
  Tmp1 :=  $SPR_{traps}$ 
[1] Repeat until Tmp1 =  $\emptyset$ 
  begin
    %  $\mathcal{T}$  is the set of traps of this
    % subprocess
    Let  $(sp, \mathcal{T}) \in Tmp1$ 
    Tmp1 := Tmp1 /  $\{(sp, \mathcal{T})\}$ 

    % for each trap in  $\mathcal{T}$ 
[2] Repeat until  $\mathcal{T} = \emptyset$ 
    begin
      Let  $tp \in \mathcal{T}$ 
       $\mathcal{T} := \mathcal{T} / \{tp\}$ 

      %  $\mathcal{S}_{tp}$  is the set of states defining
      % this trap
[3] Let  $\mathcal{S}_{tp}$  such that  $(tp, \mathcal{S}_{tp}) \in TRP_{states}$ 
      Suppose  $\mathcal{S}_{tp} = \{st_1, \dots, st_n\}$ 
[4] GenerateRule(  $\Box((sp \wedge (st_1 \vee \dots \vee st_n)) \rightarrow tp)$  )
    end % {Repeat until  $\mathcal{T} = \emptyset$ }
  end % {Repeat until Tmp1 =  $\emptyset$ }
```

### 5) Initial conditions.

INPUT:  $INI_{states}$

PROCEDURE:

```
GenerateRule( init )
Suppose  $INI_{states} = \{st_1, \dots, st_n\}$ 
[1] GenerateRule(  $init \rightarrow (st_1 \wedge \dots \wedge st_n)$  )
```

## 5.3. Complexity

It can be proved that our translation algorithm runs in polynomial time. We will develop our complexity analysis using the asymptotic notation often known as “the order of” or “big Oh” (see for example [5]). Thus we will find an upper bound for the worst-case execution time of the algorithm steps presented previously. Formally,

**DEFINITION 1** Let  $n \in \mathbb{N}$  be the size of the algorithm input and  $t : \mathbb{N} \rightarrow \mathbb{R}^{\geq 0}$  a function expressing the algorithm execution time for input  $n$ . Let  $f : \mathbb{N} \rightarrow \mathbb{R}^{\geq 0}$  an arbitrary function, then  $t$  is “in the order of”  $f$  iff  $t(n) \in O(f(n))$ , where

$$O(f(n)) = \{g : \mathbb{N} \rightarrow \mathbb{R}^{\geq 0} \mid \begin{array}{l} (\exists c \in \mathbb{R}^+) \\ (\exists n_0 \in \mathbb{N}) \\ (\forall n \geq n_0) \\ [g(n) \leq cf(n)] \end{array}\}$$

△

Therefore, we can state our claim in the asymptotic notation as:

**THEOREM 1** Let  $n$  be the size of a given PARADIGM model  $\mathcal{M}$ , i.e. the input size for the translation algorithm. Let  $t(n)$  be the function expressing the algorithm execution time. Let  $St$ ,  $Sp$  and  $Tp$  be respectively the sets of all states, subprocesses and traps of  $\mathcal{M}$ . Let  $IS_1, \dots, IS_m$  be the input sets derived from  $\mathcal{M}$ , i.e. those sets obtained as shown in section 5.1. Then  $t(n)$  is polynomial on the size of  $n$ , where  $n = \max(|St|, |Sp|, |Tp|, |IS_1|, \dots, |IS_m|)$ . ▲

We defined the model size  $n$  as being the maximum cardinality among particular sets because a) the algorithm performs its computation over different input sets and b) we must operate with a unified input size for obtaining a unique function expressing the order of the entire algorithm.

It is also worthy to mention that some execution times are considered negligible in the broader computation. These comprise assignments and the time that takes to remove an element from a set once it has already been found. In addition we assume that sets are simply implemented as lists, that all set operations are performed as sequential searches over their data structures and the time that takes to generate a rule is proportional to the number of propositions included in the rule schema.

The translation algorithm comprises five separate steps (see section 5.2, all assumed to be performed sequentially. Proving that each one of these steps runs in polynomial time allow us to infer the entire algorithm is polynomial. These partial proofs refer to some lines in the algorithm which has been marked with  $[n]$ . Function  $\max(a_1, \dots, a_n)$  returns the maximum value among  $a_1, \dots, a_n$ .  $|S|$  denotes the cardinality of set  $S$ .

**LEMMA 1** Rules expressing state changes in employee processes (see step 1 in section 5.2) can be generated in  $O(n^5)$ . ▲

*Sketch of proof 1* The order of step 1 is

$$O_{step1} = L_o.max(O_2, O_3) \quad (1)$$

where  $L_o$  is the number of iterations of the outer loop (line [1]),

$$L_o = |Tmp1| = |EMP| \leq n \quad (2)$$

and  $O_2$  is the order of a search over  $PRO_{transitions}$  (line [2]),

$$O_2 = n \quad (3)$$

and  $O_3$  is the order of the inner loop (line [3]),

$$O_3 = L_i.max(O_4, O_5, O_6, O_7, O_8) \quad (4)$$

where  $L_i$  is the number of iterations of the inner loop (line [3]),  $L_i = |Tmp2| = |\mathcal{T}_e|$ , where  $\mathcal{T}_e$  is the set of transitions in employee  $e$ ,

$$L_i \leq n \quad (5)$$

and  $O_4$  is the order of a search over  $TRP_{subprocesses}$  (line [4]),

$$O_4 = n \quad (6)$$

and  $O_5$  is the order of a search over  $EMP_{subprocesses}$  (line [5]),

$$O_5 = n \quad (7)$$

and  $O_6$  is the order of the time that takes to compose set  $\mathcal{S}_{ij}^M$  (line [6]), which involves an intersection-inclusion proof for every element of set  $\mathcal{S}_e$ ,

$$O_6 = |\mathcal{S}_e|.max(O_\cap, O_\subset) \quad (8)$$

where  $O_\cap$  is the order of the time that takes to perform  $\mathcal{S}_m \cap \mathcal{S}_{ij}$ , which in turn can be bounded by  $|\mathcal{S}_m| \cdot |\mathcal{S}_{ij}|$ . As  $|\mathcal{S}_m|$  is at most the maximum number of subprocesses that can be prescribed by a manager to a single employee, and  $|\mathcal{S}_{ij}|$  is at most the maximum of subprocesses a given transition is part of, then  $|\mathcal{S}_m| \leq n$  and  $|\mathcal{S}_{ij}| \leq n$ , then

$$O_\cap = n^2 \quad (9)$$

and  $O_\subset$  is the order of the time that takes to perform  $\mathcal{I} \subset \mathcal{S}_m$ , which in turn can be bounded by  $|\mathcal{I}| \cdot |\mathcal{S}_m|$ . As  $|\mathcal{I}|$  is at most  $|\mathcal{S}_m| \leq n$ , then

$$O_\subset = n^2 \quad (10)$$

and  $|\mathcal{S}_e|$  is at most the maximum number of managers for a given employee,

$$|\mathcal{S}_e| \leq n \quad (11)$$

$O_7$  refers to the set  $\mathcal{J}$  of other outgoing transitions from the same state. This construction, and related operations like the search over the Generated set can be proved to be subsumed by  $O_6$ .

$O_8$  is the order of the time that takes to generate the rule (line [8]). We can see the number of elements to be written in the PLTL program is clearly dominated by  $|\mathcal{S}_{ij}^M|$ , which in turn is at most  $|\mathcal{S}_e| \leq n$  and then

$$O_8 = n \quad (12)$$

From eqs. 9, 10, 11 and 12 we have that  $O_6 = n^3$  (eq. 8).

From eqs. 5, 6, 7 and 8 we have that  $O_3 = n^4$  (eq. 4).

From eqs. 2, 3 and 4 we have that  $O_{step1} = n^5$  (eq. 1).  $\triangle$

**LEMMA 2** Rules expressing subprocess prescriptions in manager states (see step 2 in section 5.2) can be generated in  $O(n^2)$ .  $\blacktriangle$

*Sketch of proof 2* The order of step 2 is

$$O_{step2} = L_o.O_2 \quad (13)$$

where  $L_o$  is the number of iterations of the outer loop (line [1]),

$$L_o = |Tmp1| = |MAN_{subprocesses}| \leq n \quad (14)$$

and  $O_2$  is the order of the time that takes to generate the rule (line [2]). We can see the number of elements to be written in the PLTL program is clearly dominated by  $\neg \mathcal{S}_{st}$ , which in turn is at most the maximum number of subprocesses that a manager can prescribe on a single state, and then

$$O_2 = n \quad (15)$$

From eqs. 14 and 15 we have that  $O_{step2} = n^2$  (eq. 13).  $\triangle$

**LEMMA 3** Rules expressing state changes in manager processes (see step 3 in section 5.2) can be generated in  $O(n^4)$ .  $\blacktriangle$

*Sketch of proof 3* The order of step 3 is

$$O_{step3} = L_o.max(O_2, O_3) \quad (16)$$

where  $L_o$  is the number of iterations of the outer loop (line [1]),

$$L_o = |Tmp1| = |MAN| \leq n \quad (17)$$

and  $O_2$  is the order of a search over  $PRO_{transitions}$  (line [2]),

$$O_2 = n \quad (18)$$

and  $O_3$  is the order of the inner loop (line [3]),

$$O_3 = L_i.max(O_4, O_5, O_6, O_7, O_8, O_9) \quad (19)$$

where  $L_i$  is the number of iterations of the inner loop (line [3]). As  $L_i = |Tmp2| = |\mathcal{T}_m|$ , where  $\mathcal{T}_m$  is the set of transitions in manager  $m$ , then

$$L_i \leq n \quad (20)$$

and  $O_4$  is the order of a search over  $MAN_{traps}$  (line [4]),

$$O_4 = n \quad (21)$$

and  $O_5 = O_6$  is the order of a search over  $MAN_{subprocesses}$  (lines [5] and [6]),

$$O_5 = O_6 = n \quad (22)$$

and  $O_7$  is the order of the time that takes to compose the set  $\mathcal{D}$ , which in turn involves the time that takes to perform the difference  $\mathcal{I}_m/\mathcal{J}$  (line[7]). As this time is bounded by  $|\mathcal{I}| \cdot |\mathcal{J}|$  and  $|\mathcal{I}|$  and  $|\mathcal{J}|$  are at most the maximum number of subprocesses that can be prescribed by a manager to a single employee, then  $|\mathcal{I}| \leq n$  and  $|\mathcal{J}| \leq n$  so

$$O_7 = n^2 \quad (23)$$

and  $O_8$  is the order of the time that takes to compose set  $\mathcal{T}_{left}$  (line [8]), which involves a search over  $SPR_{traps}$  for every element of set  $\mathcal{D}$ . This time is bounded by  $|\mathcal{D}| \cdot |SPR_{traps}| \leq n^2$ , and then

$$O_8 = n^2 \quad (24)$$

and  $O_9$  is the order of the time that takes to generate the rule (line [9]). We can see the number of elements to be written in the PLTL program is clearly dominated by  $|\mathcal{T}_{ij}| + |\mathcal{D}| + |\mathcal{T}_{left}|$ . These cardinalities are at most the maximum number of employees for any manager, the maximum number of subprocesses that can be prescribed on a single manager state and the maximum number of traps in the PARADIGMmodel respectively. Therefore, the time of generation is at most  $3n$  yielding

$$O_9 = n \quad (25)$$

From eqs. 20, 21, 22, 23, 24 and 25 we have that  $O_3 = n^3$  (eq. 19).

From eqs. 17 and 18 we have that  $O_{step3} = n^4$  (eq. 16).  $\triangle$

**LEMMA 4** Rules expressing state changes in manager processes (see step 4 in section 5.2) can be generated in  $O(n^3)$ .  $\blacktriangle$

*Sketch of proof 4* The order of step 4 is

$$O_{step4} = L_o \cdot O_i \quad (26)$$

where  $L_o$  is the number of iterations of the outer loop (line [1]),

$$L_o = |Tmp1| = |SPR_{traps}| \leq n \quad (27)$$

and  $O_i$  is the order of the inner loop (line [2]),

$$O_i = L_i \cdot \max(O_3, O_4) \quad (28)$$

where  $L_i$  is the number of iterations of the inner loop, this is  $L_i = |Tmp2| = |\mathcal{T}|$  where  $|\mathcal{T}|$  is at most the maximum number of traps in any subprocess, and then

$$L_i \leq n \quad (29)$$

and  $O_3$  is the order of a search over  $TRP_{states}$  (line [3]),

$$O_3 = n \quad (30)$$

and  $O_4$  is the order of the time that takes to generate the rule (line [4]). We can see the number of elements to be written in the PLTL program is clearly dominated by  $|\mathcal{S}_{tp}|$ , which in turn is at most the maximum number of states defining a trap, less or equal than  $n$  and then

$$O_4 = n \quad (31)$$

From eqs. 29, 30 and 31 we have that  $O_i = n^2$  (eq. 28).

From eqs. 27 and 28 we have that  $O_{step4} = n^3$  (eq. 26).  $\triangle$

**LEMMA 5** Rules expressing initial conditions (see step 5 in section 5.2) can be generated in  $O(n)$ .  $\blacktriangle$

*Sketch of proof 5* Clearly, the order of step 5 is dominated by the generation time (line [1]) which in turn is proportional to the number of processes in the PARADIGMmodel. As this number is less or equal than  $n$ , step 5 is  $O(n)$ .  $\triangle$

Theorems 1, 2, 3, 4 and 5 support our claim, i.e., the entire translation algorithm runs in polynomial time. In fact, it is at most  $O(n^5)$ .

## 6. AN EXAMPLE

Next we show a PLTL program generated by the translation of the partial specification of the ATM case study. Also remember although manager ATM is also involved with subprocess checkPIN, we are just focusing on manager BankComputer to illustrate the algorithm. We remind the reader a full version of the example and the corresponding set of rules is available in [2].

% STATE CHANGES IN EMPLOYEE PROCESSES

% in checkPIN()

```

□((cpChecked ∧ cps1) →
  ◇(¬ cpChecked ∧ cpNotChecking))
□((cpNotChecking ∧ cps2) →
  ◇(¬ cpNotChecking ∧ cpConnected))
□((cpVerifying ∧ cps3) →
  ◇(¬ cpVerifying ∧ cpChecked))
□((cpConnected ∧ cps4) →
  ◇(¬ cpConnected ∧ cpVerifying))

```

```

% in verifyAccount()

□((vaAccountOK ∧ vAs1) →
  ◇(¬ vaAccountOK ∧ vaNotVerifying))
□((vaAccountNotOK ∧ vAs1) →
  ◇(¬ vaAccountNotOK ∧ vaNotVerifying))
□((vaNotVerifying ∧ vAs2) →
  ◇(¬ vaNotVerifying ∧ vaEncrypted))
□((vaEncrypted ∧ vAs2) →
  ◇(¬ vaEncrypted
    ∧
    (vaAccountOK ⊕ vaAccountNotOK)))

```

% SUBPROCESS PRESCRIPTIONS

% by manager BankComputer

```

□(bcWaiting → (cPs4 ∧ gMs4 ∧ pTs1 ∧ vAs1))
□(bcVerifying → (cPs4 ∧ gMs4 ∧ pTs1 ∧ vAs2))

```

% STATE CHANGES IN MANAGER PROCESSES

% in BankComputer

```

□((bcWaiting ∧ tcP4 ∧ tvA1) →
  ◇(¬ bcWaiting ∧ bcVerifying ∧
    ¬ vAs1 ∧ ¬ tvA1))

```

% INSIDE TRAPS

% belonging to checkPIN()

```

□((cPs1 ∧ cpNotChecking) → tcP1)
□((cPs2 ∧
  (cpConnected ∨ cpVerifying ∨ cpChecked)
  → tcP2)
□((cPs3 ∧
  (cpNotChecking ∨ cpConnected ∨ cpChecked)
  → tcP3)
□((cPs4 ∧ cpVerifying) → tcP4)

```

% belonging to verifyAccount()

```

□((vAs1 ∧ vaNotVerifying) → tvA1)
□((vAs2 ∧ vaAccountOK) → tvA2)
□((vAs2 ∧ vaAccountNotOK) → tvA3)

```

% INITIAL CONDITIONS

init

```

init →
(cpNotChecking ∧ vaNotVerifying ∧ bcWaiting ∧ ...)

```

## 7. MODEL VERIFICATION

This section shows that is possible to link the PLTL program resulting from the translation, to a verification procedure about correctness in the initial PARADIGM model. We show that well-known properties in the system verification literature [12] can be naturally expressed in the PLTL program. Further research is needed to link these notions to the already available tools SPIN and STeP.

**EXAMPLE 6** (*safety property*) “Any account can be either accepted or rejected, but it can never be in both states”

$\Box \neg (vaAccountOK \wedge vaAccountNotOK) \quad \Delta$

**EXAMPLE 7** (*guarantee property*) “It is possible for the ATM to report a PIN as checked while BankComputer is still verifying it.”

$\Diamond (cpChecked \wedge vAs2) \quad \Delta$

**EXAMPLE 8** (*response properties*) “All PIN verifications will eventually end”

$\Box (cpVerifying \rightarrow \Diamond cpChecked)$

“If ATM requests BankComputer to verify a PIN, it always gets an answer, either positive or negative”

$\Box (tcP4 \rightarrow \Diamond (tvA2 \vee tvA3))$

$\Delta$

**EXAMPLE 9** (*response/recurrence property*) “The stage of verifying account implies to check if the account is acceptable or not. After that step the process is re-started.”

$\Box (vaNotVerifying \rightarrow$   
 $\quad \Diamond ((vaAccountOK \oplus vaAccountNotOK)$   
 $\quad \wedge$   
 $\quad \Diamond vaNotVerifying))$

$\Delta$

**EXAMPLE 10** A recurrence property: “The process of checking a PIN can be cyclically invoked”

$\Box (\Diamond cpNotChecking \wedge \Diamond \neg cpNotChecking)$

However, some readers may find the following two rules easier to understand:

$\Box (\Diamond (cpNotChecking \wedge \Diamond \neg cpNotChecking))$

$\Box (\Diamond (\neg cpNotChecking \wedge \Diamond cpNotChecking)) \quad \Delta$

It can be seen that the verification process can be set, either at the more general level of the functionality of the system (examples 6 and 9) or at a subtler level of traps and subprocesses (examples 7 and 8). Our PLTL translation can be coupled more or less easily with a PLTL interpreter to verify temporal properties. Other alternatives includes the consideration of systems like STeP and SPIN. As mentioned earlier, SPIN is based on model checking. Because in this technique the space of possible states of the global automata is explored the tool is restricted to finite state systems. On the other hand highly efficient algorithms made this tool very successful for industrial applications. STeP instead is a collection of tools mainly focused on a deductive approach to verification, although also provides model checking support. Being a deductive system it can deal with infinite state specifications and hence, providing better scalability than tools centered on state-exploration like SPIN.

As our work addresses some temporal aspects implicit in PARADIGM specifications, it may help to encode these notions in Fair Transition Systems, in the case of STeP, or global automata, in the case of SPIN. We also believe that our specification language may be linked to other verification frameworks. Indeed, Etessami [9] discusses a translation of an extended version of Linear Temporal Logic (LTL) to Büchi Automata.

## 8. CONCLUSIONS

We have introduced a translation process that takes a PARADIGM model and generates a PLTL program which expresses, from a declarative approach, the dynamic behavior of described by the model. This program can be used to trace process interactions and verify, to a certain extent, correctness properties. For example, classical properties such as guarantee, persistence, response and others can be queried to verify correctness of PARADIGM models.

We focused on a polynomial translation algorithm (a Prolog implementation is discussed in [2]). We complement a previous conference paper ([3]) which introduced the main concepts behind the translation process and its application in system verification. This work is certainly worth to be compared with [10], where a transition-like operational semantics is considered. However algorithms and verification possibilities are not addressed in depth.

Further work is needed to link PARADIGM with verification tools like Step and SPIN, but nevertheless we have revealed some important insights on the dynamic aspects of PARADIGM models. This will hopefully encourage further research on verification of PARADIGM-modelled systems.

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