Delayed switching applied to memristor neural networks

Frank Z. Wang,1,a) Na Helian,2 Yike Guo,2 Sining Wu,1 Xiao Yang,1 Guan Lim,1 and Md Mamunur Rashid4

1Future Computing Group, School of Computing, University of Kent, United Kingdom
2School of Computer Science, University of Hertfordshire, United Kingdom
3Department of Computing, Imperial College, United Kingdom
4CERN, Geneva, Switzerland

(Presented 3 November 2011; received 28 September 2011; accepted 26 October 2011; published online xx xx xxxx)

Magnetic flux and electric charge are linked in a memristor. We reported recently that a memristor has a peculiar effect in which the switching takes place with a time delay because a memristor possesses a certain inertia. This effect was named the “delayed switching effect.” In this work, we elaborate on the importance of delayed switching in a brain-like computer using memristor neural networks. The effect is used to control the switching of a memristor synapse between two neurons that fire together (the Hebbian rule). A theoretical formula is found, and the design is verified by a simulation. We have also built an experimental setup consisting of electronic memristive synapses and electronic neurons. © 2012 American Institute of Physics. [doi:10.1063/1.3672409]

I. INTRODUCTION

Since the first computer was built, scientists have been fascinated with the idea of a computer that works similarly as the human brain. However, all previous efforts at building brain-like computers failed because it took about the same silicon area to emulate a CMOS synapse as was needed to emulate a neuron. In a typical human brain, there are 1011 neurons and 1014 synapses (on average, each neuron is connected to other neurons through about 20,000 synapses). Any realistic implementation of a synapse should ideally be at least four orders of magnitude smaller than that required to build a neuron. Although the implementation of a neuron is relatively easier, an electronic synapse is not so straightforward to make for the above-stated reason.

The invention of the memristor1 provides a new way to implement synapses. A memristor is a simple 2-terminal element, which means a vast number of memristors could be integrated together with other CMOS elements in a single chip. A LaAlO3/SrTiO3 junction presents a uni-polar pinched hysteresis loop and also provides the potential for a memristor to be scaled down to half a nanometer.2 Memristors are passive and non-volatile and consume much less power.

Naturally, the freezing memory property by which a memristor stores resistance value makes memristors suitable for use as synapses. As shown in Fig. 1(b), the switching from high resistance (Roh) to low resistance (Ron) takes place with a time delay Td after the application of an input voltage. In a memristor neural network, a square-wave signal is equivalent, in terms of switching a memristor synapse, to a sequence of spikes with the same net area as the observation region bounded by the graph of the signal and the time axis (Fig. 1(c)). This is because charge is the time integral of current, and the mem-resistance is normally a function of charge.

The resistance of a memristor depends on the complete past history of the current, i.e., the time integral of the current from τ = −∞ to τ = t. As mentioned above, the current (voltage) is a sequence of spikes with a frequency f and a (equal) spike width Tw. Therefore,

\[ q(t) = \int_{-\infty}^{t} i(\tau) d\tau = \int_{-\infty}^{t} \frac{V d\tau}{R} = \frac{V}{R} \cdot T_w \cdot f \cdot t. \]  (1)

At the transition where \( t = T_{d1,2} \), we have \( q(T_{d1,2}) = Q_{1,2} \) and \( φ(T_{d1,2}) = φ_{1,2} \). Therefore,

\[ Q_{1,2} = \frac{V}{ φ_{1,2}} \cdot T_w \cdot f \cdot T_{d1,2}, \]  (2)

\[ T_{d1,2} = \frac{φ_{1,2}}{V \cdot T_w \cdot f}, \quad T_{d1} = \frac{φ_{1}}{V \cdot T_w \cdot f}, \quad T_{d2} = \frac{φ_{2}}{V \cdot T_w \cdot f}. \]  (3)

Equation (3) clearly demonstrates that \( T_d \) decreases with an increased spike amplitude \( V \), an increased spike width \( T_w \), or an increased spike frequency \( f \). If the input voltage is removed before the switching takes place, i.e., the width \( T \) of the input voltage pulse is smaller than \( T_d \approx T_{d1} \approx T_{d2} \), the memristor remains unaltered. Therefore, in order to switch a memristor, \( T \) should be chosen in such a way that \( T > T_d \).

II. DELAYED SWITCH IN MEMRISTOR NEURAL NETWORKS

As shown in Fig. 2, we consider a simplified neural network comprising three neurons (N1, N2, and N3) coupled by two memristive synapses (S1 and S2). This network can perform the Pavlovian experiment on conditioned reflex. The first input neuron (presumably located in the visual cortex) activates under a specific visual event, such as “sight of food,” and the second input neuron (presumably located in...
the auditory cortex) activates under an external auditory event, such as “sound of bell.” Depending on previous training, each of these events can trigger “salivation” (firing of the third output neuron). If, at a certain moment in time, only the sight of food leads to salivation, and subsequently the circuit is subjected to both input events, then, after a sufficient number of simultaneous input events, the circuit starts associating the sound of a bell with the sight of food, and eventually it begins to salivate upon the activation of the sound only. This process of learning is a realization of the famous Hebbian rule.

A biological neuron behaves like an analog-to-digital converter. When a neuron receives a receptor potential exceeding a threshold value, it starts emitting both forward (along the output terminal of the neuron) and backward (along the input of the neuron) action spikes; the amplitude of these spikes is constant, but their frequency depends on the stimulus strength.

A biological synapse is a connection that permits a neuron to pass an electrical signal to another neuron. Our memristor synapse is modeled in Fig. 1(a). As shown in Fig. 2, the synapse S1 receives a voltage determined by the output of the neuron N1 at its front (forward-propagating spikes) and the input of another neuron N3 at its back (backward-propagating spikes). If the pre-synaptic and post-synaptic spikes overlap, a positive “half voltage” (+v/2) and a negative “half voltage” (−v/2) generate a “full voltage” drop (v) across the synapse.

The simulation results are shown in Fig. 3. The width of each pulse (spike) is set at 4 time units, and the memristor synapse S2 remains unaltered (still disconnected). The simulation period is 6600 time units.

In the “probing” phase (“food” only or “bell” only in Fig. 3), the salivation neuron fires only when a stimulus signal is applied to the sight neuron, as S1 is connected and S2 is disconnected.

In the “learning” phase (Fig. 3), stimulus voltages are applied simultaneously to both input neurons (“sight” and “sound”), thus generating a sequence of spikes. The spikes from different neurons are uncorrelated, but sometimes they do overlap, owing to a random component in the spike separation. During this phase, in some moments of time, back-propagating spikes from the salivation neuron (due to excitation from the sight neuron) overlap with forward propagating spikes from the sound neuron, causing a full voltage across the second memristor synapse S2. As this voltage exceeds the memristor threshold, S2 changes its state and switches into a low resistance state (connection). It is important to note that this change is possible when both stimuli are applied together (in other words, they correlate). As a result, an association between input stimuli develops, and the

FIG. 2. (Color online) A neural network using memristors as synapses. When a neuron fires, it starts emitting a forward spike, +V/2, and a backward spike, −V/2. The strengths of memristor synapses can be modified when these two spikes overlap.

FIG. 3. (Color online) Simulation demonstration of the memristor neural network in Fig. 2.
network “learns” to associate the sight neuron with the sound neuron.

Our measurements during the second probing phase (“validation” in Fig. 3) clearly demonstrate the developed association. In this phase, any type of stimulus, whether from the sight neuron or from the sound neuron, results in the firing of the salivation neuron.

If the width of each spike is increased to 16 time units (with the same frequency), the integral (charge) rises quickly and the memristor time delay (Eq. (3)) is overtaken; as a result, S2 will change its state even under a half voltage (only the sound neuron fires), as shown in Fig. 4. Obviously this is a mis-operation in which the sound neuron is connected with the salivation neuron by mistake, violating the Hebbian rule (“neurons that fire together, wire together”).

III. CIRCUIT EXPERIMENTS

Based on Chua’s “circuit-model,” we have built an experimental setup consisting of electronic memristive synapses and electronic neurons. The electronic memristor synapse can be tuned to represent the functions found in biological neural cells.

The waveforms are measured with a 16 to 25 Hz square-wave input signal, a low resistance of 625 kΩ, and a high resistance of 10 kΩ. As shown in Fig. 5, the application of the delayed switching in a neural network has been achieved.

IV. CONCLUSION

A memristor mimics the synapses between the neurons in the brain in terms of being plastic according to the dynamical history of the system. According to Eq. (3), the sequence length, sequence frequency, and spike width need to be carefully controlled in such a way that the memristor synapse time delay point is not be overtaken while only one neuron fires.

ACKNOWLEDGMENTS

This research was conducted with partial support from UK Government EPSRC Grant (EP/E064930/1). The authors wish to thank Professor Leon Chua (University of California) for his helpful comments and suggestions while he was a Leverhulme Trust Visiting Professor in the UK over the past year.